Homework 5, Linear Systems, Fall 2008

- When turn in your homework, please write down: 作業次別, 姓名, 學號, 系級, 日期
- Assigned: 12/17/08, Due on 12/24/08
- (Minimal Realization)
 - 3 (A parallel electrical circuit)

20 points

• If $L_1 = L_2, C_1 = C_2, R_1 = R_2$, and c = [0,0,0,1], show that the state-space model is NOT a minimal realization and find a minimal realization from the state-space model. You also need to show that the realization you find is minimal.

(A 3-tank system)

20 points

• If the three-tank system is with only input u_2 and output x_2 , then A, B, C, D of the state-space model is given in the following.

$$\mathbf{A} = \begin{bmatrix} -3 & 3 & 0 \\ 2 & -4 & 2 \\ 0 & 3 & -3 \end{bmatrix}, \ \mathbf{B} = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}, \ \mathbf{C} = \begin{bmatrix} 0 & 1 & 0 \end{bmatrix}, \\ \mathbf{D} = \begin{bmatrix} 0 \end{bmatrix},$$

Show that the state-space model is NOT a minimal realization and find a minimal realization from the state-space model. You also need to show that the realization you drive is minimal.