Introduction to Electronic Design Automation

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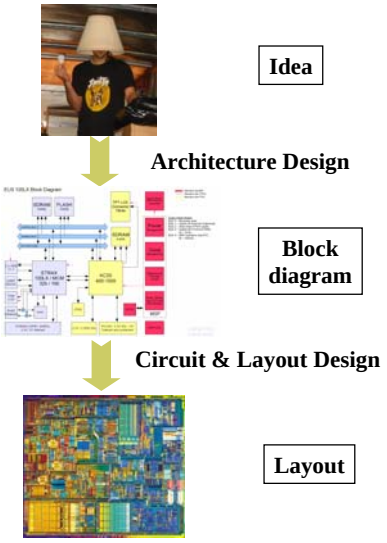
Testing

Slides are by Courtesy of Prof. S.-Y. Huang and C.-M. Li

Testing

- Recap
  - Design verification
    - Is what I specified really what I wanted?
      - Property checking
  - Implementation verification
    - Is what I implemented really what I specified?
      - Equivalence checking
  - Manufacture verification
    - Is what I manufactured really what I implemented?
      - Testing; post manufacture verification
      - Quality control
        - Distinguish between good and bad chips

Design Flow



Manufacturing Defects

- Processing faults
  - missing contact windows
  - parasitic transistors
  - oxide breakdown
- Material defects
  - bulk defects (cracks, crystal imperfections)
  - surface impurities
- Time-dependent failures
  - dielectric breakdown
  - electro-migration
- Packaging failures
  - contact degradation
  - seal leaks

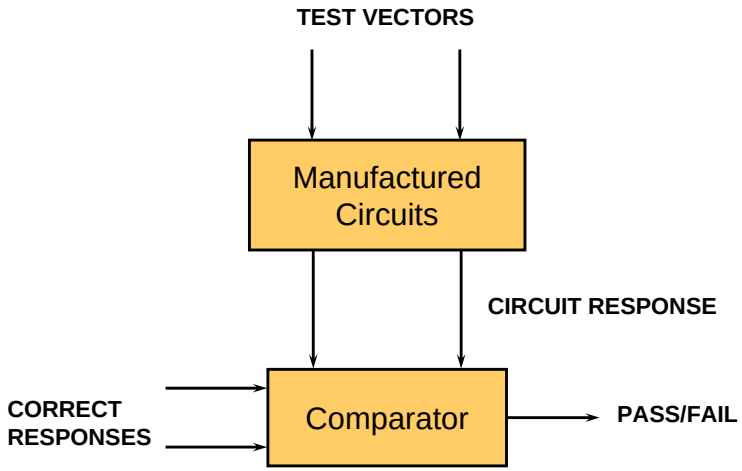
Faults, Errors and Failures

- Faults
  - A physical defect within a circuit or a system
  - May or may not cause a system failure
- Errors
  - Manifestation of a fault that results in incorrect circuit (system) outputs or states
  - Caused by faults
- Failures
  - Deviation of a circuit or system from its specified behavior
  - Fail to do what is supposed to do
  - Caused by errors
- Faults cause errors; errors cause failures

Testing and Diagnosis

- Testing
  - Exercise a system and analyze the response to ensure whether it behaves correctly after manufacturing
- Diagnosis
  - Locate the causes of misbehavior after the incorrectness is detected

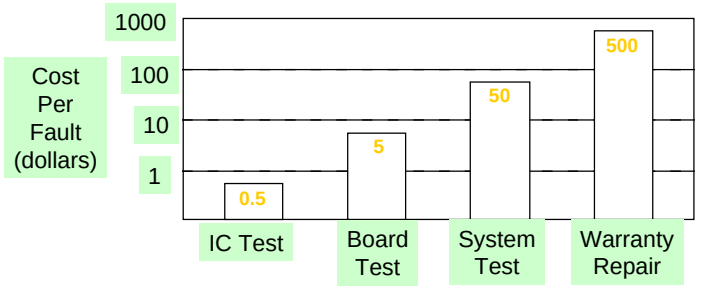
Scenario of Manufacturing Test



Test Systems

Purpose of Testing

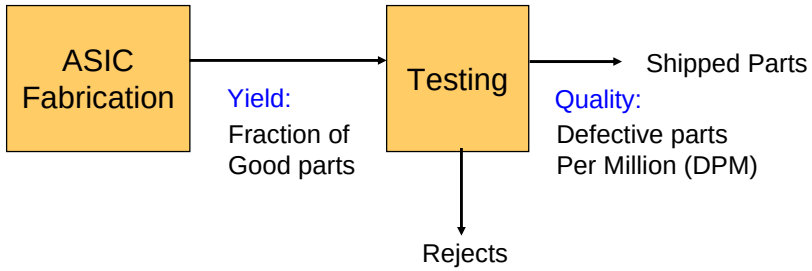
- Verify manufactured circuits
  - Improve system reliability
  - Reduce repair costs
    - Repair cost goes up by an order of magnitude each step away from the fab. line



B. Davis, "The Economics of Automatic Testing" McGraw-Hill 1982

Testing and Quality

- Quality of shipped part can be expressed as a function of the yield Y and test (fault) coverage T.



Fault Coverage

- Fault coverage T
  - Measure of the ability of a test set to detect a given set of faults that may occur on the Design Under Test (DUT)

$$T = \frac{\text{\# detected faults}}{\text{\# all possible faults}}$$

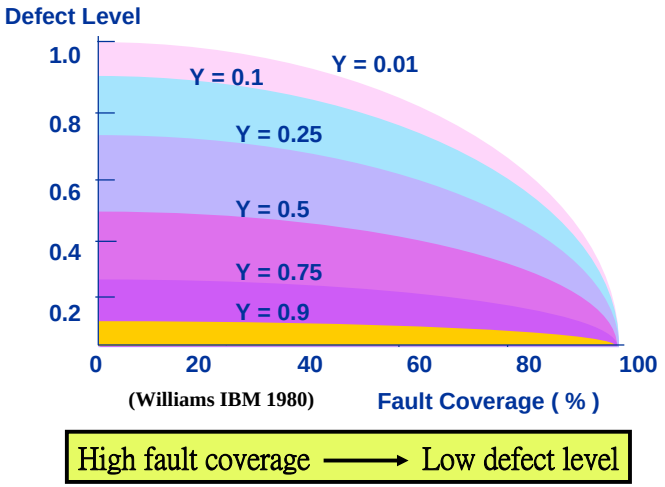
Defect Level

- A defect level is the fraction of the shipped parts that are defective

$$DL = 1 - Y^{(1-T)}$$

Y: yield
T: fault coverage

Defect Level vs. Fault Coverage



High fault coverage ⟶ Low defect level

DPM vs. Yield and Coverage

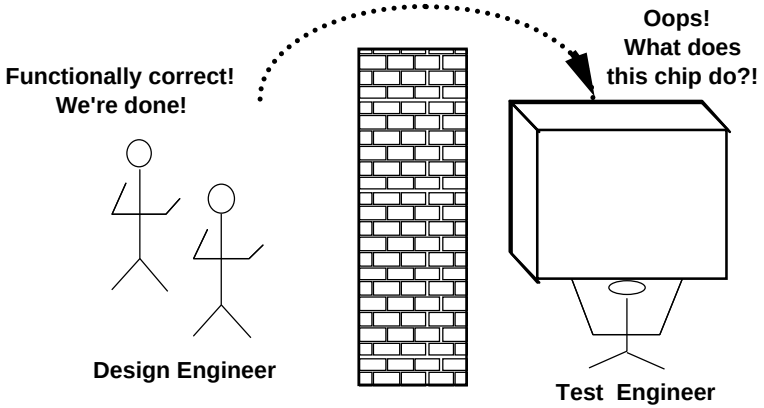
Yield	Fault Coverage	DPM
50%	**90%**	**67,000**
75%	**90%**	**28,000**
90%	**90%**	**10,000**
95%	**90%**	**5,000**
99%	**90%**	**1,000**
90%	**90%**	**10,000**
90%	**95%**	**5,000**
90%	**99%**	**1,000**
90%	**99.9%**	**100**

Why Testing Is Difficult ?

- Test time explodes exponentially in exhaustive testing of VLSI
  - For a combinational circuit with 50 inputs, need 2^{50} = 1.126×10^{15} test patterns.
  - Assume one test per 10^{-7}sec, it takes 1.125×10^{8}sec = 3.57years.
  - Test generation for sequential circuits are even more difficult due to the lack of controllability and observability at flip-flops (latches)
- Functional testing
  - may NOT be able to detect the physical faults

The Infamous Design/Test Wall

30-years of experience proves that
test after design does not work!



Outline

- Fault Modeling
- Fault Simulation
- Automatic Test Pattern Generation
- Design for Testability

Functional vs. Structural Testing

- I/O functional testing is inadequate for manufacturing
  - Need fault models
- Exhaustive testing is daunting
  - Need abstraction and smart algorithms
  - Structural testing is more effective

Why Fault Model ?

- Fault model identifies target faults
  - Model faults that are most likely to occur
- Fault model limits the scope of test generation
  - Create tests only for the modeled faults
- Fault model makes testing effective
  - Fault coverage can be computed for specific test patterns to measure its effectiveness
- Fault model makes analysis possible
  - Associate specific defects with specific test patterns

Fault Modeling vs. Physical Defects

- Fault modeling
  - Model the effects of physical defects on the logic function and timing
- Physical defects
  - Silicon defects
  - Photolithographic defects
  - Mask contamination
  - Process variation
  - Defective oxides

Fault Modeling vs. Physical Defects (cont'd)

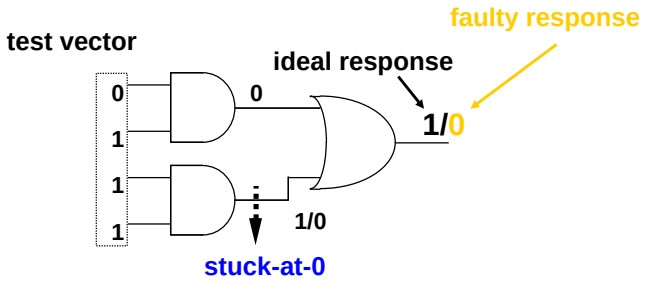
- Electrical effects
  - Shorts (bridging faults)
  - Opens
  - Transistor stuck-on/open
  - Resistive shorts/opens
  - Change in threshold voltages
- Logical effects
  - Logical stuck-at-0/1
  - Slower transition (delay faults)
  - AND-bridging, OR-bridging

Typical Fault Types

- **Stuck-at faults**
- Bridging faults
- Transistor stuck-on/open faults
- Delay faults
- IDDQ faults
- State transition faults (for FSM)
- Memory faults
- PLA faults

Single Stuck-At Fault

- Assumptions:
  - Only one wire is faulty
  - Fault can be at an input or output of a gate
  - Faulty wire permanently sticks at 0 or 1



Multiple Stuck-At Faults

- Several stuck-at faults occur at the same time
  - Common in high density circuits
- For a circuit with *k* lines
  - There are $2k$ single stuck-at faults
  - There are 3^k-1 multiple stuck-at faults
    - A line could be stuck-at-0, stuck-at-1, or fault-free
    - One out of 3^k resulting circuits is fault-free

Why Single Stuck-At Fault Model ?

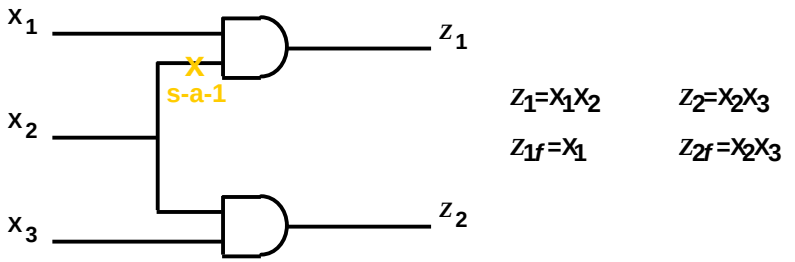
- Complexity is greatly reduced
  - Many different physical defects may be modeled by the same logical single stuck-at fault
- Stuck-at fault is technology independent
  - Can be applied to TTL, ECL, CMOS, BiCMOS etc.
- Design style independent
  - Gate array, standard cell, custom design
- Detection capability of un-modeled defects
  - Empirically, many un-modeled defects can also be detected accidentally under the single stuck-at fault model
- Cover a large percentage of multiple stuck-at faults

Why Logical Fault Modeling ?

- Fault analysis on logic rather than physical problem
  - Complexity is reduced
- Technology independent
  - Same fault model is applicable to many technologies
  - Testing and diagnosis methods remain valid despite changes in technology
- Wide applications
  - The derived tests may be used for physical faults whose effect on circuit behavior is not completely understood or too complex to be analyzed
- Popularity
  - Stuck-at fault is the most popular logical fault model

Definition of Fault Detection

- A test (vector) *t* detects a fault *f* iff *t* detects *f* (i.e. $z(t) \neq z_f(t)$)
- Example

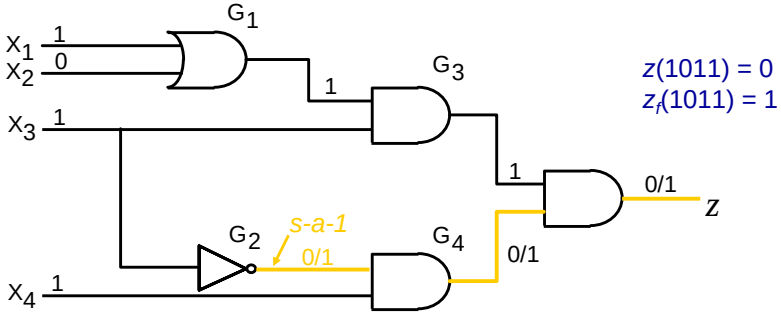


Test (x1,x2,x3) = (100) detects *f* because $z_1(100)=0$ and $z_{1f}(100)=1$

Fault Detection Requirement

- A test *t* that detects a fault *f*
  - activates *f* (or generate a fault effect) by creating different *v* and v_f values at the site of the fault
  - propagates the error to a primary output *z* by making all the wires along at least one path between the fault site and *z* have different *v* and v_f values
- Sensitized wire
  - A wire whose value in response to the test changes in the presence of the fault *f* is said to be sensitized by the test in the faulty circuit
- Sensitized path
  - A path composed of sensitized wires is called a sensitized path

Fault Sensitization



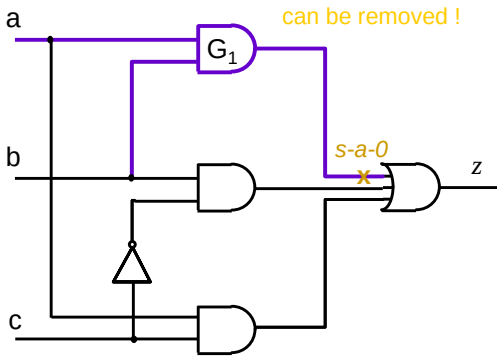
Input vector 1011 detects the fault *f* (G_2 stuck-at-1)
v/v_f : *v* = signal value in the fault free circuit
v_f = signal value in the faulty circuit

Detectability

- A fault *f* is said to be detectable
  - if there exists a test *t* that detects *f*
  - otherwise, *f* is an undetectable fault
- For an undetectable fault *f*
  - no test can simultaneously activate *f* and create a sensitized path to some primary output

Undetectable Fault

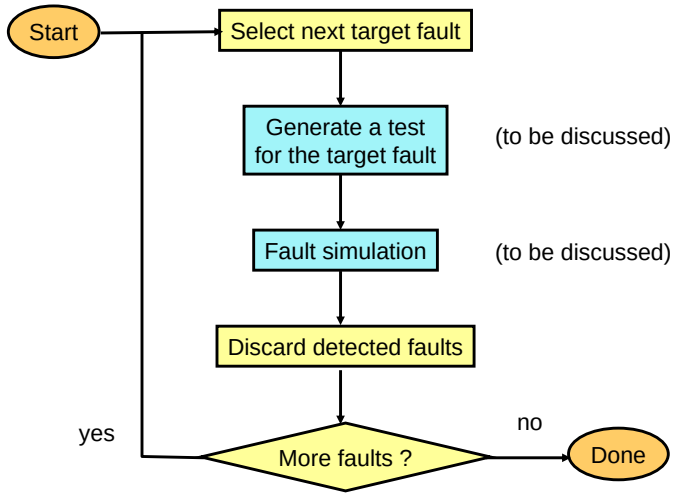
- The stuck-at-0 fault at G_1 output is undetectable
  - Undetectable faults do not change the function of the circuit
  - The related circuit can be deleted to simplify the circuit



Test Set

- Complete detection test set
  - A set of tests that detects any detectable fault in a designated set of faults
- Quality of a test set
  - is measured by fault coverage
- Fault coverage
  - Fraction of the faults detected by a test set
  - can be determined by fault simulation
  - >95% is typically required under the single stuck-at fault model
  - >99.9% required in the ICs manufactured by IBM

Typical Test Generation Flow

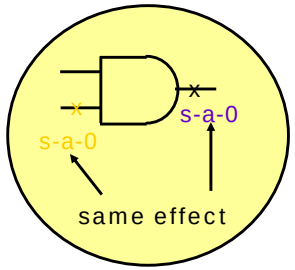


Fault Equivalence

- Distinguishing test
  - A test t distinguishes faults α and β if $z_\alpha(t) \neq z_\beta(t)$ for some PO function z
- Equivalent faults
  - Two faults α and β are said to be equivalent in a circuit iff the function under α is equal to the function under β for every input assignment (sequence) of the circuit.
  - That is, no test can distinguish α and β, i.e., test-set(α) = test-set(β)

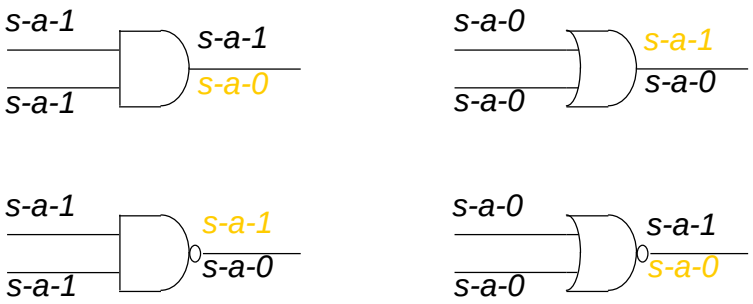
Fault Equivalence

- AND gate:
  - all *s-a-0* faults are equivalent
- OR gate:
  - all *s-a-1* faults are equivalent
- NAND gate:
  - all the input *s-a-0* faults and the output *s-a-1* faults are equivalent
- NOR gate:
  - all input *s-a-1* faults and the output *s-a-0* faults are equivalent
- Inverter:
  - input *s-a-1* and output *s-a-0* are equivalent
  - input *s-a-0* and output *s-a-1* are equivalent



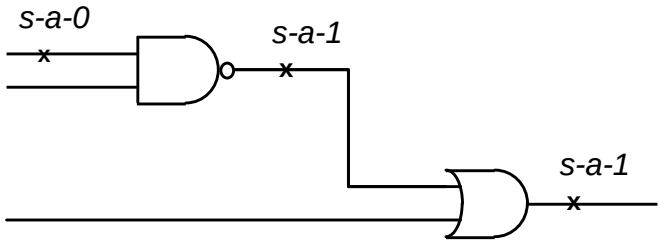
Equivalence Fault Collapsing

- *n+2*, instead of *2(n+1)*, single stuck-at faults need to be considered for *n*-input AND (or OR) gates



Equivalent Fault Group

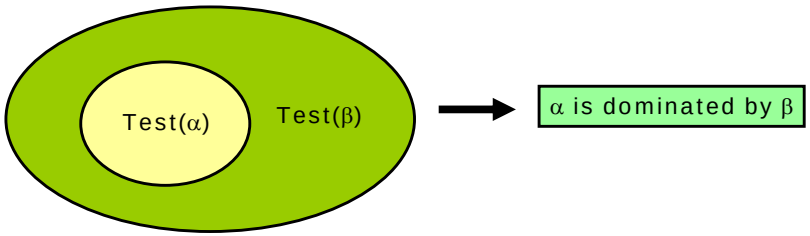
- In a combinational circuit
  - Many faults may form an equivalence group
  - These equivalent faults can be found in a reversed topological order from POs to PIs



Three faults shown are equivalent !

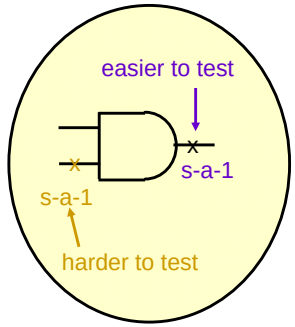
Fault Dominance

- Dominance relation
  - A fault β is said to *dominate* another fault α in an irredundant circuit iff every test (sequence) for α is also a test (sequence) for β, i.e., test-set(α) $\subseteq$ test-set(β)
  - No need to consider fault β for fault detection



Fault Dominance

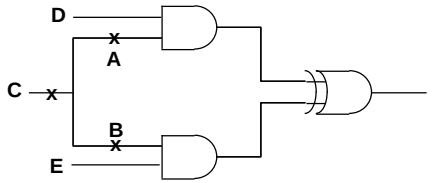
- AND gate
  - Output *s-a-1* dominates any input *s-a-1*
- NAND gate
  - Output *s-a-0* dominates any input *s-a-1*
- OR gate
  - Output *s-a-0* dominates any input *s-a-0*
- NOR gate
  - Output *s-a-1* dominates any input *s-a-0*



- Dominance fault collapsing
  - Reducing the set of faults to be analyzed based on the dominance relation

Stem vs. Branch Faults

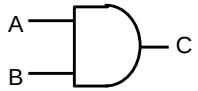
- Detect A s-a-1:
  $z(t) \oplus z_f(t) = (CD \oplus CE) \oplus (D \oplus CE) = D \oplus CD \Rightarrow (C=0, D=1)$
- Detect C s-a-1:
  $z(t) \oplus z_f(t) = (CD \oplus CE) \oplus (D \oplus E) \Rightarrow (C=0, D=1, E=0)$ or $(C=0, D=0, E=1)$
- Hence, C s-a-1 does not dominate A s-a-1
- In general, there might be no equivalence or dominance relations between stem and branch faults



C: stem of a multiple fanout
A, B: branches

Analysis of a Single Gate

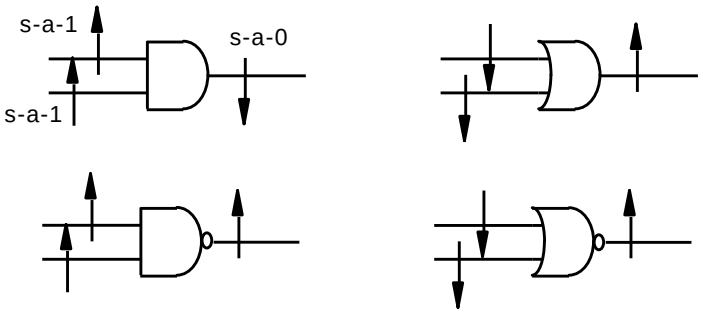
- Fault Equivalence Class
  - (A s-a-0, B s-a-0, C s-a-0)
- Fault Dominance Relations
  - (C s-a-1 > A s-a-1) and (C s-a-1 > B s-a-1)
- Faults that can be ignored:
  - A s-a-0, B s-a-0, and C s-a-1



AB	C	A sa1	B sa1	C sa1	A sa0	B sa0	C sa0
00	0			1			
01	0	1		1			
10	0		1	1			
11	1				0	0	0

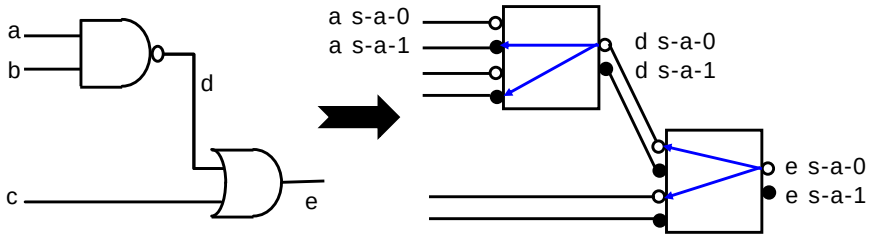
Fault Collapsing

- Collapse faults by fault equivalence and dominance
  - For an *n*-input gate, we only need to consider *n+1* faults in test generation

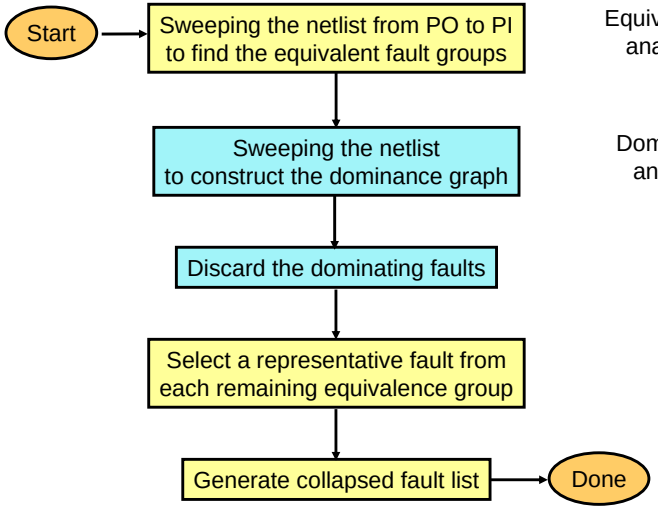


Dominance Graph

- Rule
  - When fault α dominates fault β, then an arrow is pointing from α to β
- Application
  - Find out the transitive dominance relations among faults



Fault Collapsing Flow

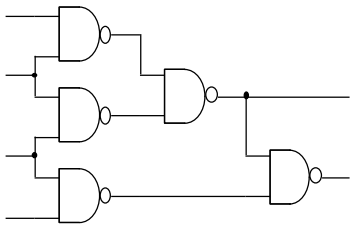


Prime Fault

- α is a prime fault if every fault that is dominated by α is also equivalent to α
- Representative Set of Prime Fault (RSPF)
  - A set that consists of exactly one prime fault from each equivalence class of prime faults
  - True minimal RSPF is difficult to find

Why Fault Collapsing ?

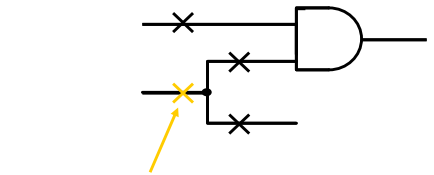
- Save memory and CPU time
- Ease testing generation and fault simulation
- Exercise



* 30 total faults → 12 prime faults

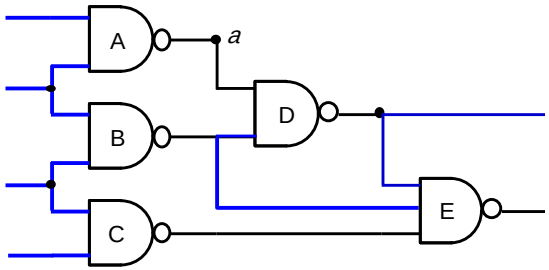
Checkpoint Theorem

- Checkpoints for test generation
  - A test set detects every fault on the primary inputs and fanout branches is complete
    - I.e., this test set detects all other faults, too
  - Therefore, primary inputs and fanout branches form a *sufficient* set of checkpoints in test generation
    - In fanout-free combinational circuits (i.e., every gate has only one fanout), primary inputs are the checkpoints



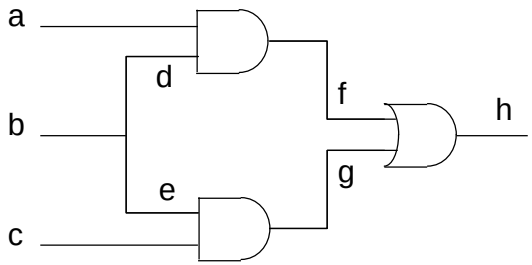
Why Inputs + Branches Are Enough ?

- Example
  - Checkpoints are marked in blue
  - Sweeping the circuit from PI to PO to examine every gate, e.g., based on an order of (A->B->C->D->E)
  - For each gate, output faults are detected if every input fault is detected



Fault Collapsing + Checkpoint

- Example:
  - 10 checkpoint faults
  - a s-a-0 <=> d s-a-0 , c s-a-0 <=> e s-a-0
    b s-a-0 > d s-a-0 , b s-a-1 > d s-a-1
  - 6 faults are enough



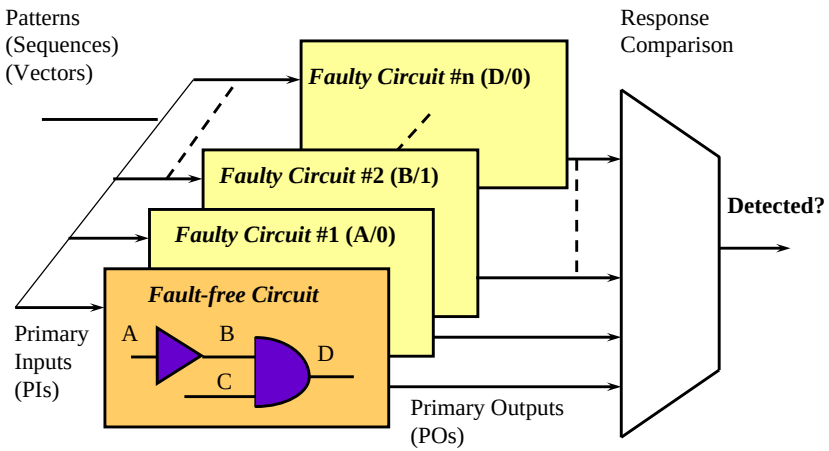
Outline

- Fault Modeling
- Fault Simulation
- Automatic Test Pattern Generation
- Design for Testability

Why Fault Simulation ?

- To evaluate the quality of a test set
  - I.e., to compute its fault coverage
- Part of an ATPG program
  - A vector usually detects multiple faults
  - Fault simulation is used to compute the faults that are accidentally detected by a particular vector
- To construct fault-dictionary
  - For post-testing diagnosis

Conceptual Fault Simulation

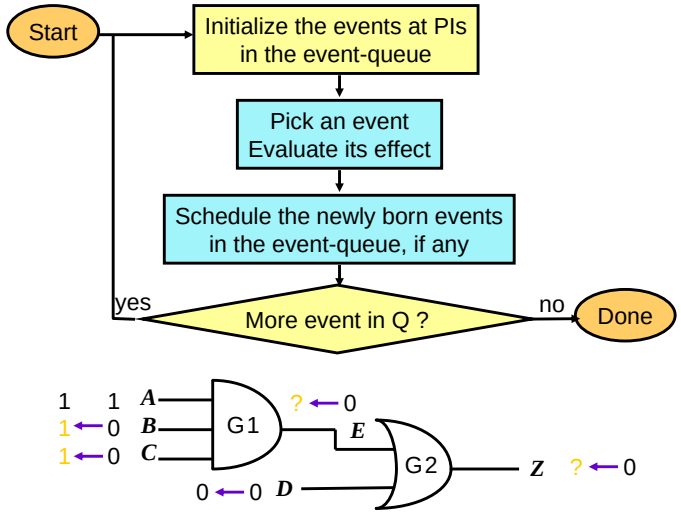


Logic simulation on both good (fault-free) and faulty circuits

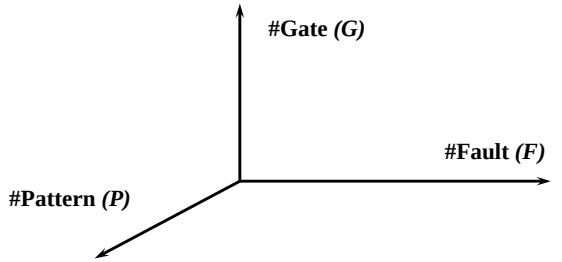
Some Basics for Logic Simulation

- In fault simulation, our main concern is functional faults; gate delays are assumed to be zero unless delay faults are considered
- Logic values can be either {0, 1} (for two-value simulation) or {0, 1, X} (for three-value simulation)
- Two simulation mechanisms:
  - Compiled-code valuation:
    - A circuit is translated into a program and all gates are executed for each pattern (may have redundant computation)
  - Event-driven valuation:
    - Simulating a vector is viewed as a sequence of value-change events propagating from PIs to POs
    - Only those logic gates affected by the events are re-evaluated

Event-Driven Simulation



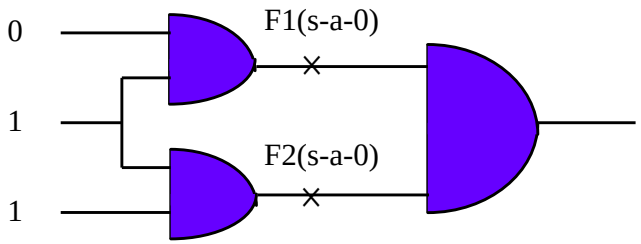
Complexity of Fault Simulation



- Complexity ~ $F \cdot P \cdot G$ ~ $O(G^3)$
- The complexity is higher than logic simulation by a factor of F, while it is usually much lower than ATPG
- The complexity can be greatly reduced using
  - fault collapsing and other advanced techniques

Characteristics of Fault Simulation

- Fault activity with respect to fault-free circuit
  - is often sparse both in time and space.
- For example
  - F1 is not activated by the given pattern, while F2 affects only the lower part of this circuit.



Fault Simulation Techniques

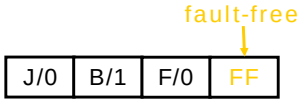
- Parallel Fault Simulation
- Deductive Fault Simulation

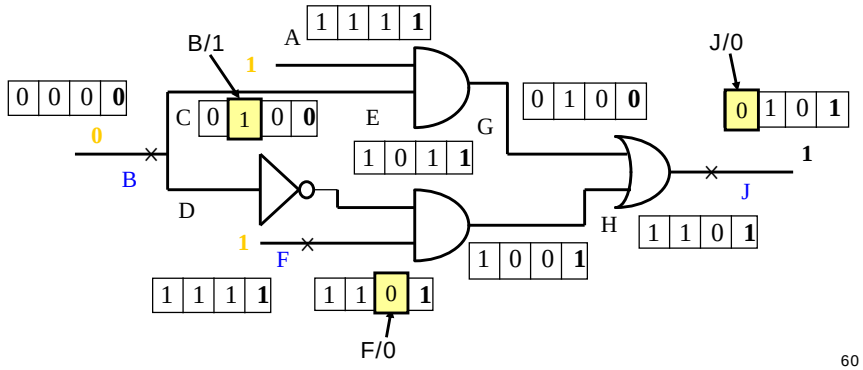
Parallel Fault Simulation

- Simulate multiple circuits simultaneously
  - The inherent parallel operation of computer words to simulate faulty circuits in parallel with fault-free circuit
  - The number of faulty circuits or faults can be processed simultaneously is limited by the word length, e.g., 32 circuits for a 32-bit computer
- Complication
  - An event or a value change of a single faulty or fault-free circuit leads to the computation of an entire word
  - The fault-free logic simulation is repeated for each pass

Parallel Fault Simulation

- Example
  - Consider three faults: (J s-a-0, B s-a-1, and F s-a-0)
  - Bit-space: (FF denotes fault-free)



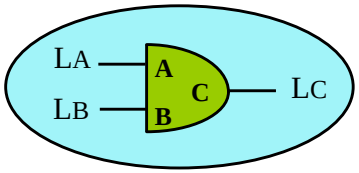


Deductive Fault Simulation

- Simulate all faulty circuits in one pass
  - For each pattern, sweep the circuit from PIs to POs.
  - During the process, a list of faults is associated with each wire
  - The list contains faults that would produce a fault effect on this wire
  - The union fault list at every PO contains the detected faults by the simulated input vector
- Main operation is fault list propagation
  - Depending on gate types and values
  - The size of the list may grow dynamically, leading to the potential memory explosion problem

Illustration of Fault List Propagation

Consider a two-input AND-gate:



Non-controlling case:

Case 1: A=1, B=1, C=1 at fault-free,
$L_C = L_A \cup L_B \cup \{C/0\}$

Controlling cases:

Case 2: A=1, B=0, C=0 at fault-free,
$L_C = (\overline{L_A} \cap L_B) \cup \{C/1\}$

Case 3: A=0, B=0, C=0 at fault-free,
$L_C = (L_A \cap L_B) \cup \{C/1\}$

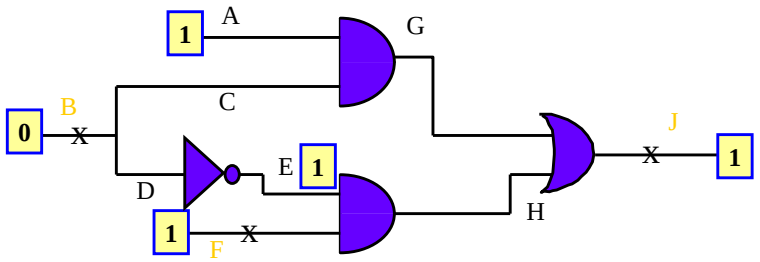
$\overline{L_A}$ is the set of all faults not in L_A

Rule of Fault List Propagation

	a	b	z	Output fault list
AND	0	0	0	$\{L_a \cap L_b\} \cup z_1$
	0	1	0	$\{L_a - L_b\} \cup z_1$
	1	0	0	$\{L_b - L_a\} \cup z_1$
	1	1	1	$\{L_a \cup L_b\} \cup z_0$
OR	0	0	0	$\{L_a \cup L_b\} \cup z_1$
	0	1	1	$\{L_b - L_a\} \cup z_0$
	1	0	1	$\{L_a - L_b\} \cup z_0$
	1	1	1	$\{L_a \cap L_b\} \cup z_0$
NOT	0		1	$L_a \cup z_0$
	1		0	$L_a \cup z_1$

Deductive Fault Simulation

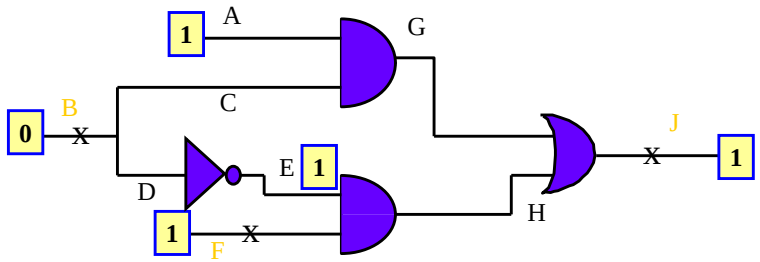
- Example (1/4)
  - Consider 3 faults: B/1, F/0, and J/0 under (A,B,F) = (1,0,1)



Fault list at PIs:
$L_B = \{B/1\}$, $L_F = \{F/0\}$, $L_A = \varnothing$, $L_C = L_D = \{B/1\}$

Deductive Fault Simulation

- Example (2/4)
  - Consider 3 faults: B/1, F/0, and J/0 under (A,B,F) = (1,0,1)



$L_B = \{B/1\}$, $L_F = \{F/0\}$, $L_A = \varnothing$, $L_C = L_D = \{B/1\}$

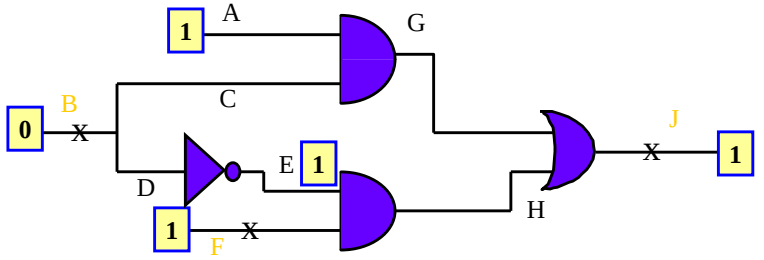
Fault lists at G and E:

$L_G = (L_A \cap L_C) \cup G/1 = \{B/1, G/1\}$

$L_E = (L_D) \cup E/0 = \{B/1, E/0\}$

Deductive Fault Simulation

- Example (3/4)
  - Consider 3 faults: B/1, F/0, and J/0 under (A,B,F) = (1,0,1)



$L_B = \{B/1\}$, $L_F = \{F/0\}$, $L_A = \varnothing$, $L_C = L_D = \{B/1\}$,

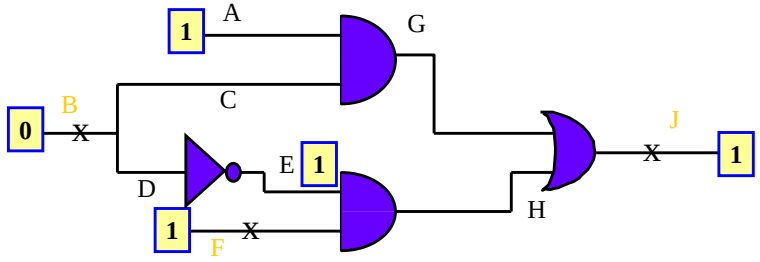
$L_G = \{B/1, G/1\}$, $L_E = \{B/1, E/0\}$

Fault list at H:

$L_H = (L_E \cup L_F) \cup L_H = \{B/1, E/0, F/0, H/0\}$

Deductive Fault Simulation

- Example (4/4)
  - Consider 3 faults: B/1, F/0, and J/0 under (A,B,F) = (1,0,1)



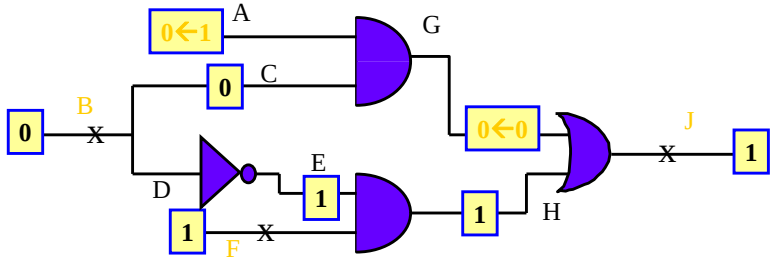
$L_B = \{B/1\}$, $L_F = \{F/0\}$, $L_A = \varnothing$, $L_C = L_D = \{B/1\}$, $L_G = \{B/1, G/1\}$, $L_E = \{B/1, E/0\}$, $L_H = \{B/1, E/0, F/0, H/0\}$

Final fault list at PO J:

$L_J = (L_H - L_G) \cup L_J = \{E/0, F/0, J/0\}$

Deductive Fault Simulation

- Example (cont'd)
  - Consider 3 faults: B/1, F/0, and J/0 under (A,B,F) = (0,0,1)



Event driven updates:

$L_B = \{B/1\}$, $L_F = \{F/0\}$, $L_A = \varnothing$, $L_C = L_D = L_E = \{B/1\}$,

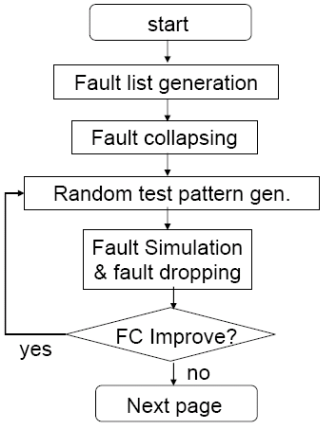
$L_G = \{G/1\}$, $L_H = \{B/1, F/0\}$, $L_J = \{B/1, F/0, J/0\}$

Outline

- Fault Modeling
- Fault Simulation
- Automatic Test Pattern Generation (ATPG)
  - Functional approach
    - Boolean difference
  - Structural approach
    - D-algorithm
    - PODEM
- Design for Testability

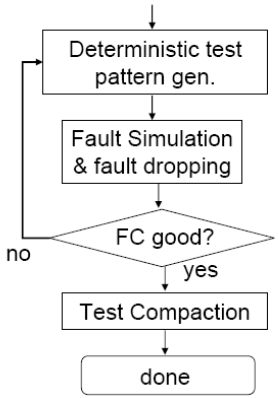
Typical ATPG Flow

- 1st phase: random test pattern generation



Typical ATPG Flow (cont'd)

- 2nd phase: deterministic test pattern generation



Test Pattern Generation

- The test set T of a fault α with respect to some PO z can be computed by

  $$T(x) = z(x) \oplus z_\alpha(x)$$

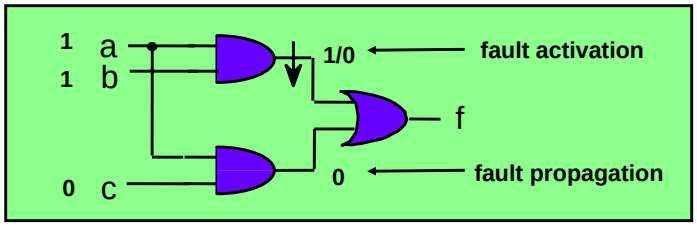
- A test pattern can be fully specified or partially specified depending on whether the values of PIs are all assigned
  - Example

abc	z	z_α
000	0	0
001	0	0
010	0	0
011	0	0
100	0	0
101	1	1
110	1	0
111	1	0

Input vectors (1,1,0) and (1,1,-) are fully and partially specified test patterns of fault α, respectively.

Structural Test Generation
D-Algorithm

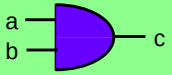
- Test generation from circuit structure
- Two basic goals
  - (1) Fault activation (FA)
  - (2) Fault propagation (FP)
  - Both of which requires Line Justification (LJ), i.e., finding input combinations that force certain signals to their desired values
- Notations:
  - 1/0 is denoted as D, meaning that good-value is 1 while faulty value is 0
  - Similarly, 0/1 is denoted D'
  - Both D and D' are called fault effects (FE)



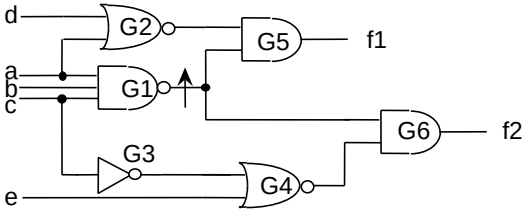
Structural Test Generation
D-Algorithm

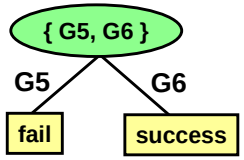
- Fault activation
  - Setting the faulty signal to either 0 or 1 is a Line Justification problem
- Fault propagation
  1. select a path to a PO → decisions
  2. once the path is selected → a set of line justification (LJ) problems are to be solved
- Line justification
  - Involves decisions or implications
  - Incorrect decisions: need backtracking

To justify c=1 → a=1 and b=1 (implication)
To justify c=0 → a=0 or b=0 (decision)



Structural Test Generation
D-Algorithm: Fault Propagation



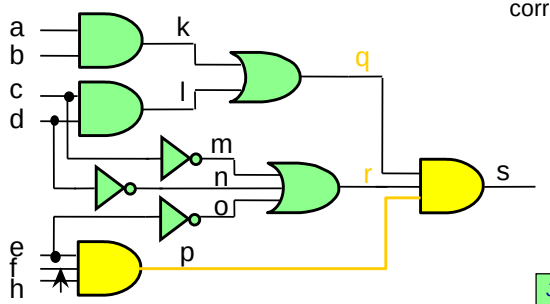


decision tree

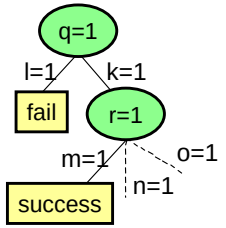
- Fault activation
  - G1=0 → { a=1, b=1, c=1 } → { G3=0 }
- Fault propagation: through G5 or G6
- Decision through G5:
  - G2=1 → { d=0, a=0 } → inconsistency at a → backtrack !!
- Decision through G6:
  - → G4=1 → e=0 → done !! The resulting test is (111x0)

D-frontiers: are the gates whose output value is x, while one or more Inputs are D or D'. For example, initially, the D-frontier is { G5, G6 }.

Structural Test Generation
D-Algorithm: Line Justification



corresponding decision tree



J-frontier: is the set of gates whose output value is known (i.e., 0 or 1), but is not implied by its input values.
Ex: initially, J-frontier is {q=1, r=1}

- FA → set h to 0
- FP → e=1, f=1 (→o=0) ; FP → q=1, r=1
- To justify q=1 → l=1 or k=1
- Decision: l =1 → c=1, d=1 → m=0, n=0 → r=0 → inconsistency at r → backtrack !
- Decision: k=1 → a=1, b=1
- To justify r=1 → m=1 or n=1 (→c=0 or d=0) → Done ! (J-frontier is ϕ)

Test Generation

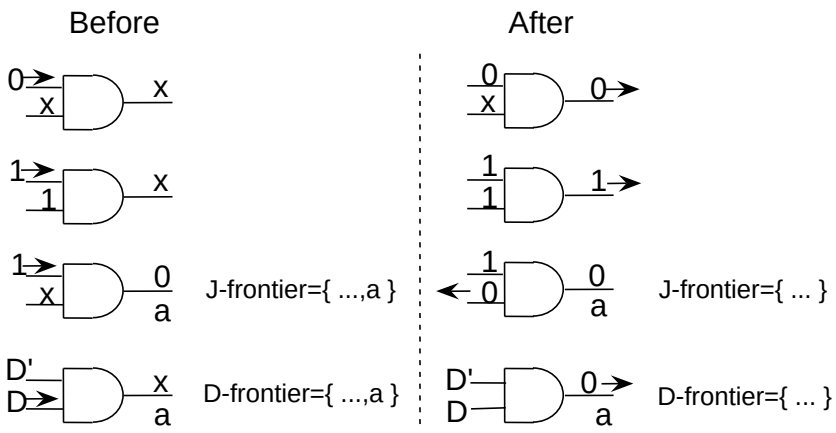
- A branch-and-bound search
- Every decision point is a branching point
- If a set of decisions lead to a conflict, a backtrack is taken to explore other decisions
- A test is found when
  1. fault effect is propagated to a PO, and
  2. all internal lines are justified
- No test is found after all possible decisions are tried → Then, target fault is undetectable
- Since the search is exhaustive, it will find a test if one exists

For a combinational circuit, an undetectable fault is also a redundant fault → Can be used to simplify circuit.

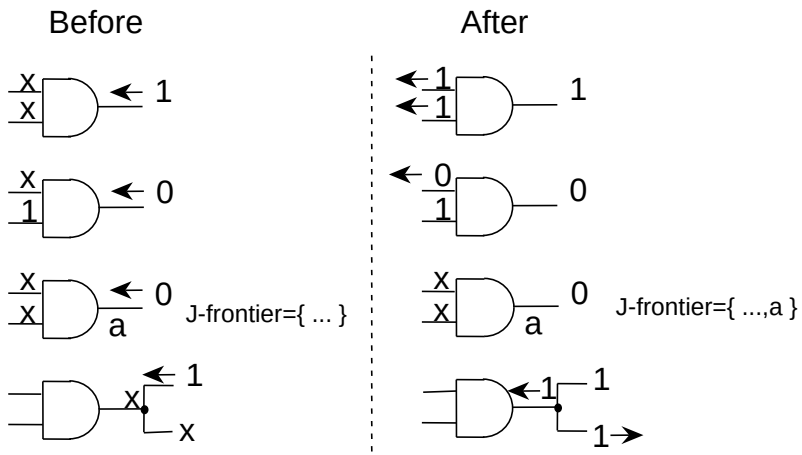
Implication

- Implication
  - Compute the values that can be uniquely determined
    - Local implication: propagation of values from one line to its immediate successors or predecessors
    - Global implication: the propagation involving a larger area of the circuit and re-convergent fanout
- Maximum implication principle
  - Perform as many implications as possible
  - It helps to either reduce the number of problems that need decisions or to reach an inconsistency sooner

Forward Implication

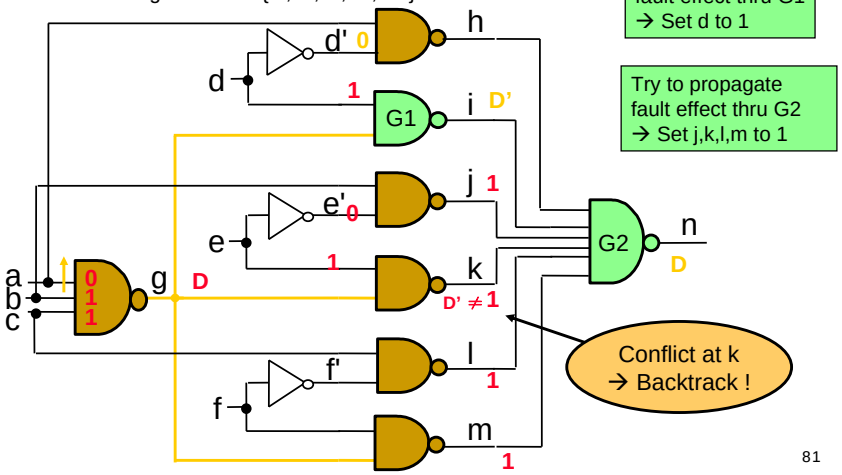


Backward Implication



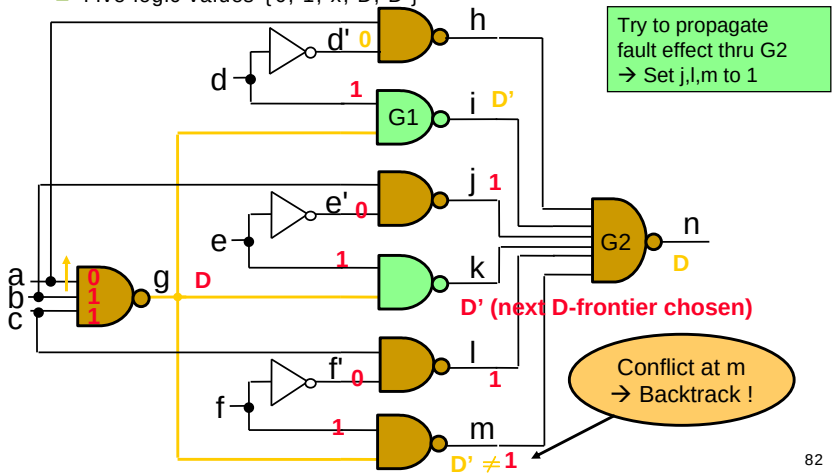
D-Algorithm (1/4)

- Example
  - Five logic values {0, 1, x, D, D'}



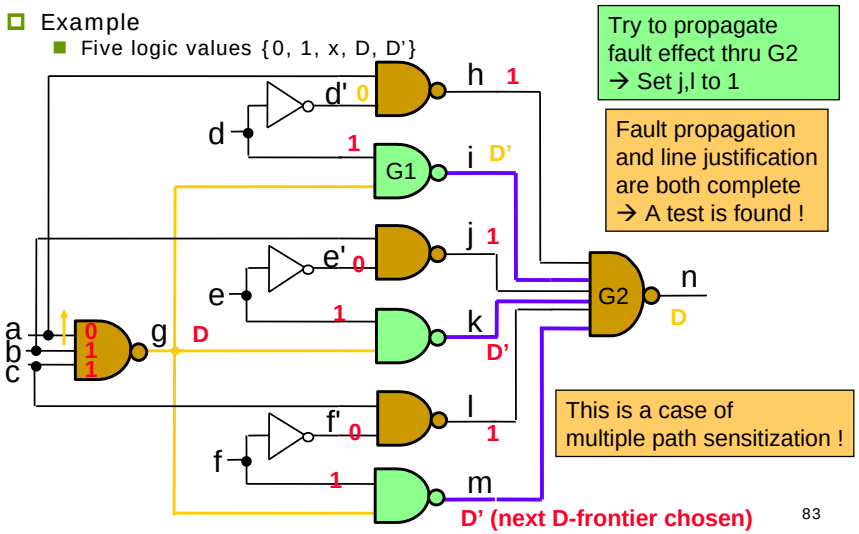
D-Algorithm (2/4)

- Example
  - Five logic values {0, 1, x, D, D'}



D-Algorithm (3/4)

- Example
  - Five logic values {0, 1, x, D, D'}



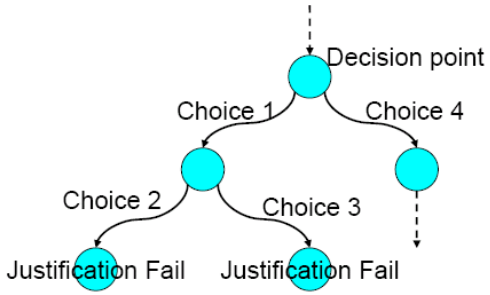
D-Algorithm (4/4)

Decision	Implication	Comments
	a=0 h=1 b=1 c=1 g=D	Active the fault Unique D-drive
d=1	i=D' d'=0	Propagate via i
j=1 k=1 l=1 m=1	n=D e'=0 e=1 k=D'	Propagate via n Contradiction

e=1	k=D' e'=0 j=1	Propagate via k
l=1 m=1	n=D f'=0 f=1 m=D'	Propagate via n Contradiction
f=1	m=D' f'=0 l=1 n=D	Propagate via m

Decision Tree on D-Frontier

- The decision tree
  - Node → D-frontier
  - Branch → decision taken
  - A Depth-First-Search (DFS) strategy is often used

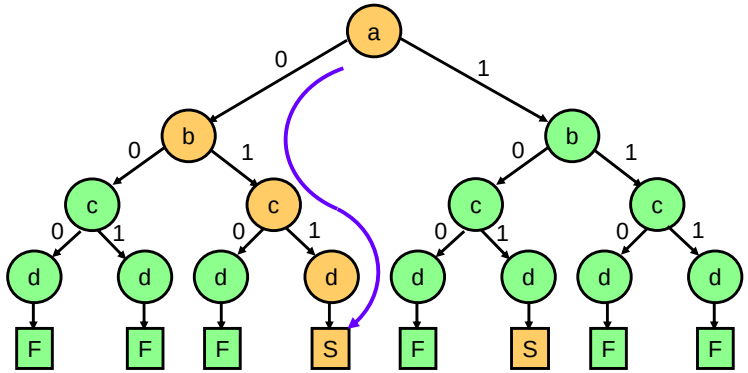


PODEM Algorithm

- PODEM: Path-Oriented DEcision Making
- Fault Activation (FA) and Propagation (FP)
  - lead to sets of Line Justification (LJ) problems. The LJ problems can be solved via value assignments.
- In D-algorithm
  - TG is done through indirect signal assignment for FA, FP, and LJ, that eventually maps into assignments at PI's
  - The decision points are at internal lines
  - The worst-case number of backtracks is exponential in terms of the number of decision points (e.g., at least 2^k for k decision nodes)
- In PODEM
  - The test generation is done through a sequence of direct assignments at PI's
  - Decision points are at PIs, thus the number of backtracking might be fewer

PODEM Algorithm
Search Space of PODEM

- Complete search space
  - A binary tree with 2^n leaf nodes, where n is the number of PIs
- Fast test generation
  - Need to find a path leading to a SUCCESS terminal quickly



PODEM Algorithm
Objective and Backtrace

- PODEM
  - Also aims at establishing a sensitization path based on fault activation and propagation like D-algorithm
  - Instead of justifying the signal values required for sensitizing the selected path, objectives are setup to guide the decision process at PIs
- Objective
  - is a signal-value pair (w, v_w)
- Backtrace
  - Backtrace maps a desired objective into a PI assignment that is likely to contribute to the achievement of the objective
  - Is a process that traverses the circuit back from the objective signal to PIs
  - The result is a PI signal-value pair (x, v_x)
  - No signal value is actually assigned during backtrace (toward PI) !

PODEM Algorithm
Objective

- Objective routine involves
  - selection of a D-frontier, G
  - selection of an unspecified input gate of G

```
Objective() {
   /* The target fault is w s-a-v */
   /* Let variable obj be a signal-value pair */
   if (the value of w is x) obj = ( w, v' );      <- fault activation
   else {
        select a gate (G) from the D-frontier;    <- fault propagation
        select an input (j) of G with value x;
        c = controlling value of G;
        obj = (j, c');
   }
   return (obj);
}
```

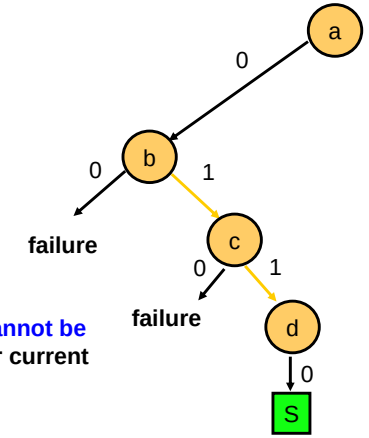

PODEM Algorithm
Backtrace

- Backtrace routine involves
  - finding an all-x path from objective site to a PI, i.e., every signal in this path has value x

```
Backtrace(w, v_w) {
   /* Maps objective into a PI assignment */
   G = w;  /* objective node */
   v = v_w; /* objective value */
   while (G is a gate output) { /* not reached PI yet */
        inv = inversion of G;
        select an input (j) of G with value x;
        G = j;          /* new objective node */
        v = v⊕inv;  /* new objective value */
   }
   /* G is a PI */    return (G, v);
}
```


PODEM Algorithm
PI Assignment

PIs: { a, b, c, d }
Current Assignments: { a=0 }
Decision: b=0 → objective fails
Reverse decision: b=1
Decision: c=0 → objective fails
Reverse decision: c=1
Decision: d=0



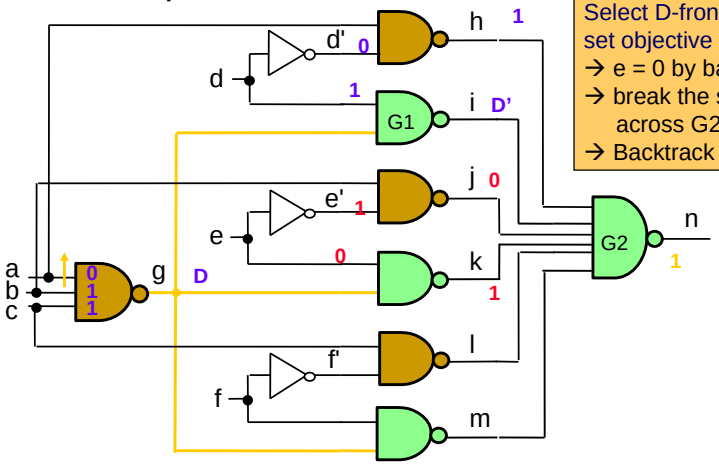
Failure means fault effect cannot be propagated to any PO under current PI assignments

PODEM Algorithm

```
PODEM () /* using depth-first-search */
begin
    If(error at PO) return(SUCCESS);
    If(test not possible)      return(FAILURE);
    (k, v_k) = Objective();            /* choose a line to be justified */
    (j, v_j) = Backtrace(k, v_k);      /* choose the PI to be assigned */
    Imply (j, v_j);                    /* make a decision */
    If ( PODEM()==SUCCESS )            return (SUCCESS);
    Imply (j, v_j');                   /* reverse decision */
    If ( PODEM()==SUCCESS )            return(SUCCESS);
    Imply (j, x);
    Return (FAILURE);
end
```

PODEM Algorithm (1/4)

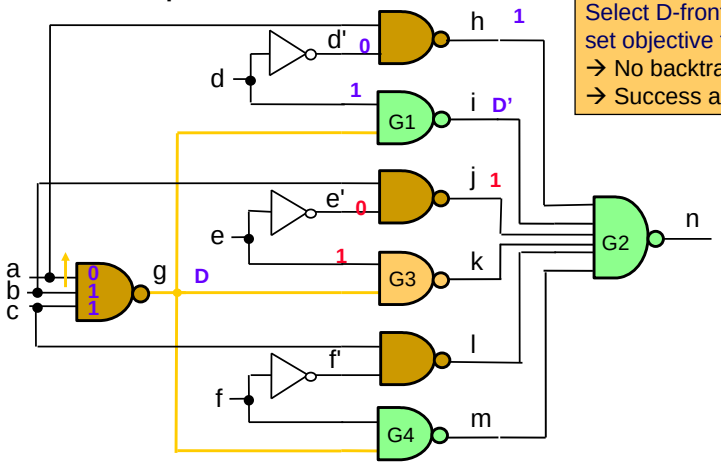
- Example



Select D-frontier G2 and set objective to (k,1)
→ e = 0 by backtrace
→ break the sensitization across G2 (j=0)
→ Backtrack !

PODEM Algorithm (2/4)

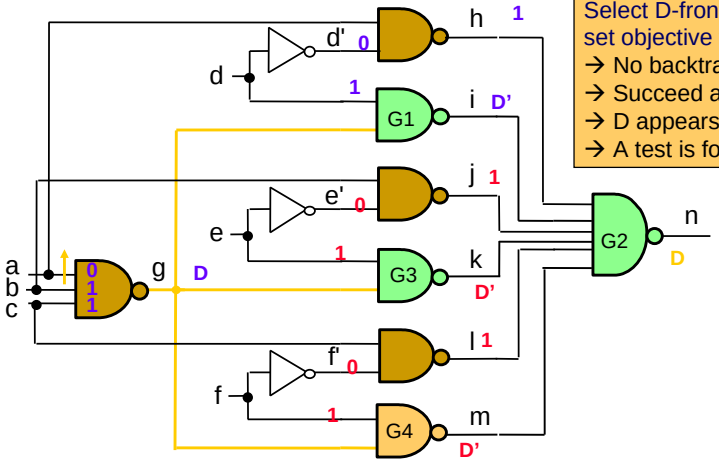
- Example



Select D-frontier G3 and set objective to (e,1)
→ No backtrace is needed
→ Success at G3

PODEM Algorithm (3/4)

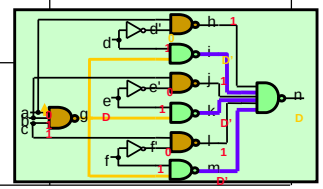
- Example



Select D-frontier G4 and set objective to (f,1)
→ No backtrace is needed
→ Succeed at G4 and G2
→ D appears at one PO
→ A test is found !!

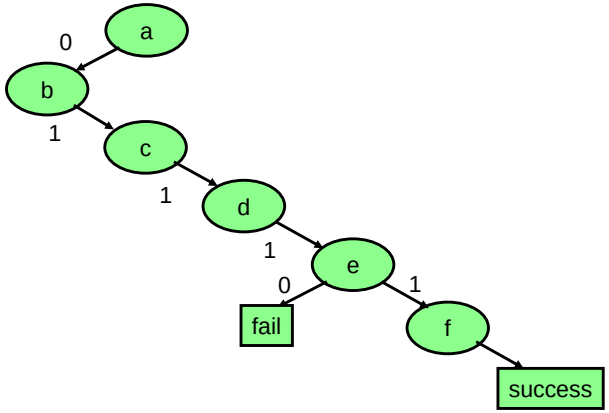
PODEM Algorithm (4/4)

Objective	PI assignment	Implications	D-frontier	Comments
a=0	a=0	h=1	g	
b=1	b=1		g	
c=1	c=1	g=D	i,k,m	
d=1	d=1	d'=0		
		i=D'	k,m,n	
k=1	e=0	e'=1 j=0 k=1 n=1	m	Assignments need to be reversed during backtracking no solutions! → backtrack
	e=1	e'=0 j=1 k=D'	m,n	flip PI assignment
l=1	f=1	f'=0 l=1 m=D' n=D		



PODEM Algorithm Decision Tree

- Decision node:
  PI selected through backtrace for value assignment
- Branch:
  value assignment to the selected PI



Termination Conditions

- D-algorithm
  - Success:
    (1) Fault effect at an output (D-frontier may not be empty)
    (2) J-frontier is empty
  - Failure:
    (1) D-frontier is empty (all possible paths are false)
    (2) J-frontier is not empty
- PODEM
  - Success:
    - Fault effect seen at an output
  - Failure:
    - Every PI assignment leads to failure, in which D-frontier is empty while fault has been activated

PODEM Overview

- PODEM
  - examines all possible input patterns implicitly but exhaustively (branch-and-bound) for finding a test
  - complete like D-algorithm (i.e., will find a test if exists)
- Other key features
  - No J-frontier, since there are no values that require justification
  - No consistency check, as conflicts can never occur
  - No backward implication, because values are propagated only forward
  - Backtracking is implicitly done by simulation rather than by an explicit and time-consuming save/restore process
  - Experiments show that PODEM is generally faster than D-algorithm

Outline

- Fault Modeling
- Fault Simulation
- Automatic Test Pattern Generation
- Design for Testability

Why DFT ?

- Direct testing is way too difficult !
  - Large number of FFs
  - Embedded memory blocks
  - Embedded analog blocks

Design for Testability

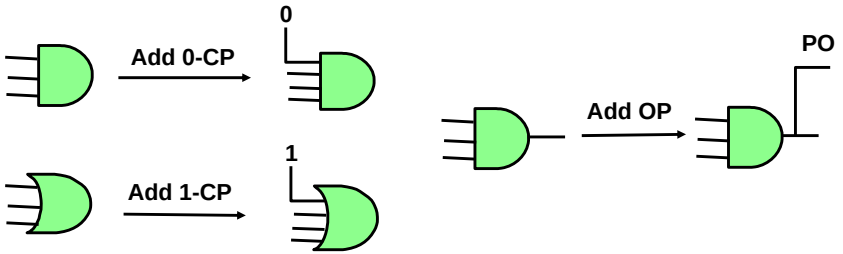
- Definition
  - Design for testability (DFT) refers to those design techniques that make test generation and testing cost-effective
- DFT methods
  - Ad-hoc methods, full and partial scan, built-in self-test (BIST), boundary scan
- Cost of DFT
  - Pin count, area, performance, design-time, test-time, etc.

Important Factors

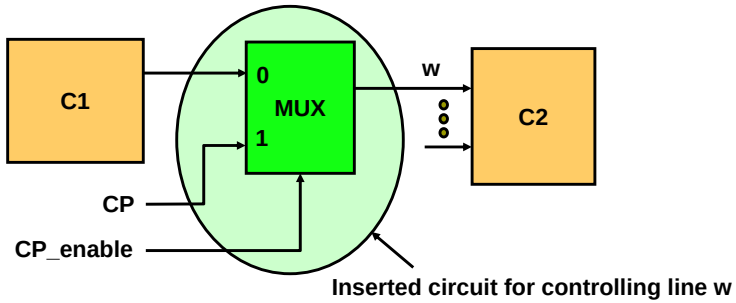
- Controllability
  - Measure the ease of controlling a line
- Observability
  - Measure the ease of observing a line at PO
- DFT deals with ways of improving
  - Controllability and observability

Test Point Insertion

- Employ test points to enhance **controllability** and **observability**
  - CP: Control Points
    - Primary inputs used to enhance controllability
  - OP: Observability Points
    - Primary outputs used to enhance observability



Control Point Insertion



- Normal operation:
  When CP_enable = 0
- Inject 0:
  Set CP_enable = 1 and CP = 0
- Inject 1:
  Set CP_enable = 1 and CP = 1

Control Point Selection

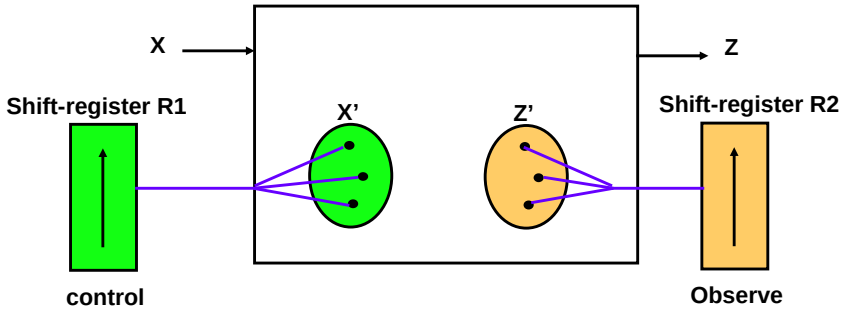
- Goal
  - Controllability of the fanout-cone of the added point is improved
- Common selections
  - Control, address, and data buses
  - Enable/hold inputs
  - Enable and read/write inputs to memory
  - Clock and preset/clear signals of flip-flops
  - Data select inputs to multiplexers and demultiplexers

Observation Point Selection

- Goal
  - Observability of the transitive fanins of the added point is improved
- Common choice
  - Stem lines with more fanouts
  - Global feedback paths
  - Redundant signal lines
  - Output of logic devices having many inputs
    - MUX, XOR trees
  - Output from state devices
  - Address, control and data buses

Problems with Test Point Insertion

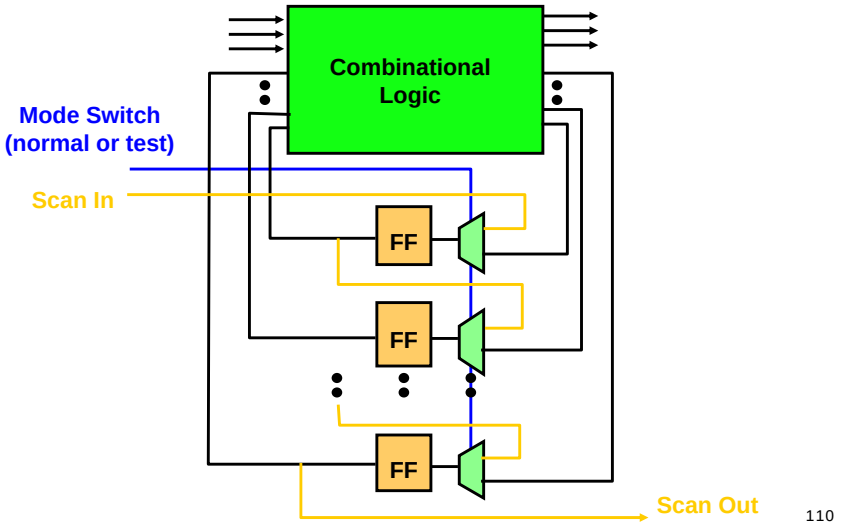
- Large number of I/O pins
  - Can be resolved by adding MUXs to reduce the number of I/O pins, or by adding shift-registers to impose CP values



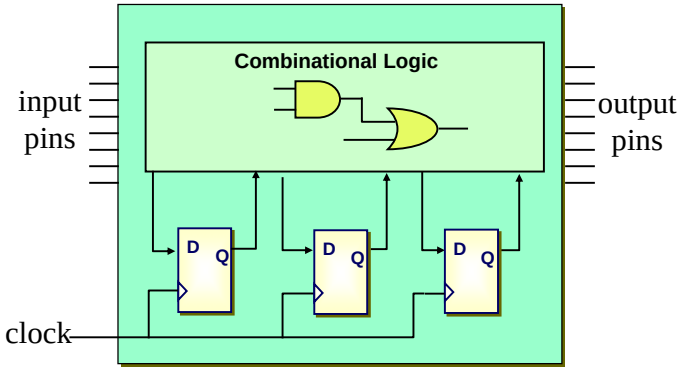
What Is Scan ?

- Objective
  - To provide controllability and observability at internal state variables for testing
- Method
  - Add test mode control signal(s) to circuit
  - Connect flip-flops to form shift registers in test mode
  - Make inputs/outputs of the flip-flops in the shift register controllable and observable
- Types
  - Internal scan
    - Full scan, partial scan, random access
  - Boundary scan

Scan Concept

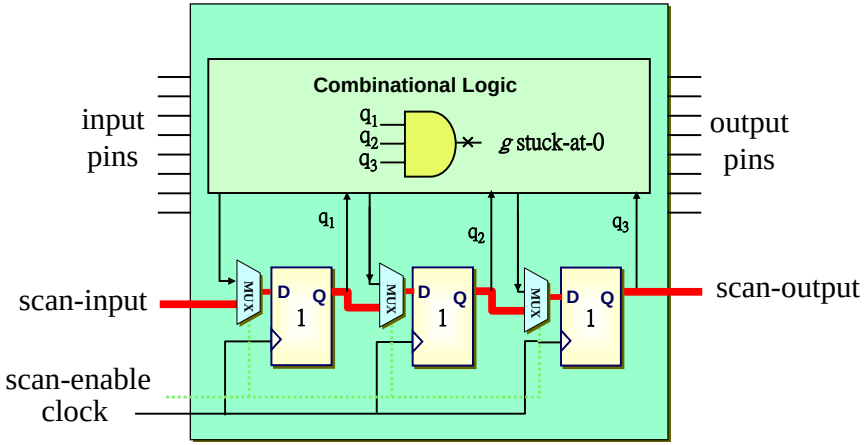


Logic Design before Scan Insertion



Sequential ATPG is extremely difficult:
due to the lack of controllability and observability at flip-flops.

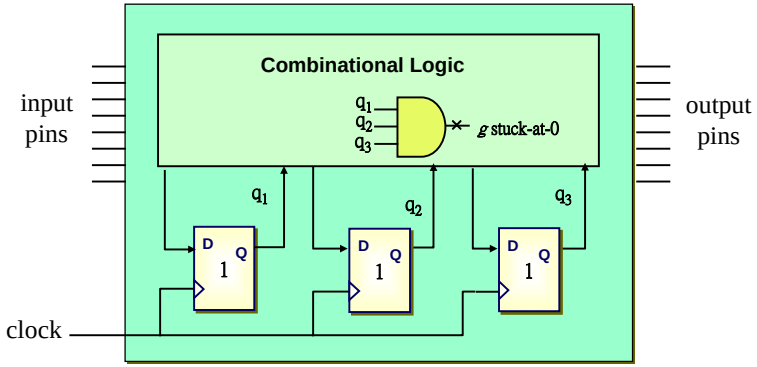
Logic Design after Scan Insertion



Scan Chain provides an easy access to flip-flops
⟶ Pattern generation is much easier !!

Scan Insertion

- Example
  - 3-stage counter



It takes 8 clock cycles to set the flip-flops to be (1, 1, 1), for detecting the target fault *g* stuck-at-0 fault (2^{20} cycles for a 20-stage counter !)

Overhead of Scan Design

- Case study
  - #CMOS gates = 2000
  - Fraction of flip-flops = 0.478
  - Fraction of normal routing = 0.471

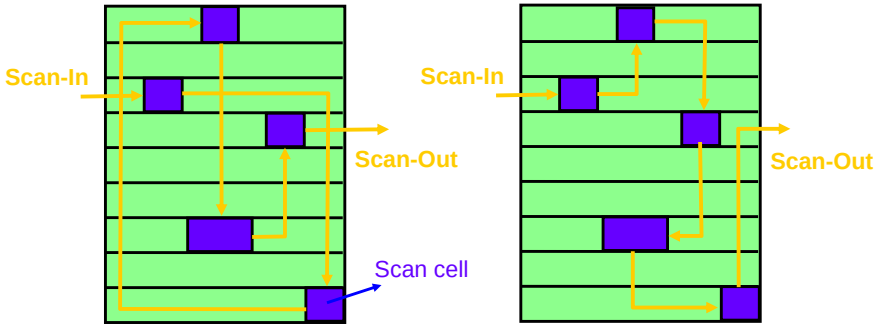
Scan implementation	Predicted overhead	Actual area overhead	Normalized operating frequency
None	0	0	1.0
Hierarchical	14.05%	16.93%	0.87
Optimized	14.05%	11.9%	0.91

Full Scan Problems

- Problems
  - Area overhead
  - Possible performance degradation
  - High test application time
  - Power dissipation
- Features of commercial tools
  - Scan-rule violation check (e.g., DFT rule check)
  - Scan insertion (convert a FF to its scan version)
  - ATPG (both combinational and sequential)
  - Scan chain reordering after layout

Scan-Chain Reordering

- Scan-chain order is often decided at gate-level without knowing the cell placement
- Scan-chain consumes a lot of routing resources, and could be minimized by re-ordering the flip-flops in the chain after layout is done



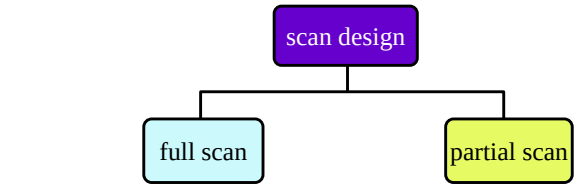
Layout of a cell-based design

A better scan-chain order

Partial Scan

- Basic idea
  - Select a subset of flip-flops for scan
  - Lower overhead (area and speed)
  - Relaxed design rules
- Cycle-breaking technique
  - Cheng & Agrawal, IEEE Trans. On Computers, April 1990
  - Select scan flip-flops to simplify sequential ATPG
  - Overhead is about 25% off than full scan
- Timing-driven partial scan
  - Jou & Cheng, ICCAD, Nov. 1991
  - Allow optimization of area, timing, and testability simultaneously

Full Scan vs. Partial Scan

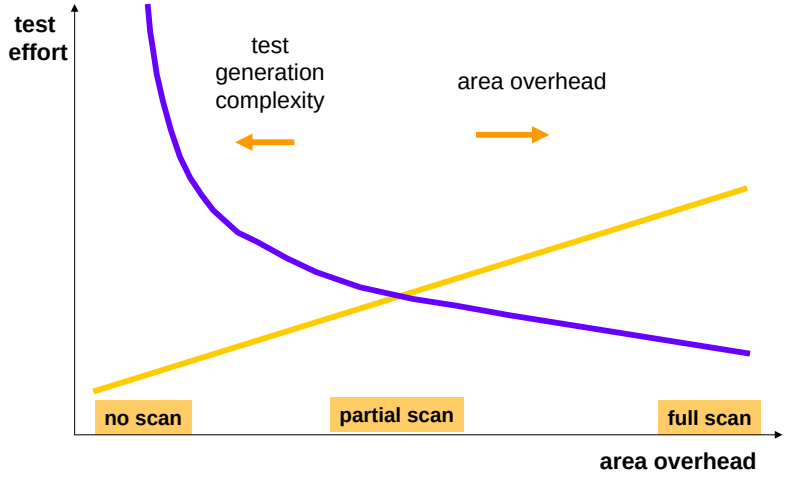


every flip-flop is a scan-FF

NOT every flip-flop is a scan-FF

scan time	longer	shorter
hardware overhead	more	less
fault coverage	~100%	unpredictable
ease-of-use	easier	harder

Area Overhead vs. Test Effort



Conclusions

- Testing
  - Conducted after manufacturing
  - Must be considered during the design process
- Major fault models
  - Stuck-at, bridging, stuck-open, delay fault, ...
- Major tools needed
  - Design-for-Testability
    - By scan chain insertion or built-in self-test
  - Fault simulation
  - ATPG
- Other Applications in CAD
  - ATPG is a way of Boolean reasoning and is applicable to may logic-domain CAD problems