

Digital Communication I

Homework 3: due 2:20pm, Nov. 19

1. Problem 5.16
2. Problem 5.30
3. Problem 5.42
4. Problem 5.43
5. In a binary phase-shift keying (PSK) modulation, the two signal waveforms are

$$\begin{aligned}s_1(t) &= \sqrt{\frac{2E}{T}} \cos[2\pi f_c t], \quad 0 \leq t \leq T \\ s_2(t) &= \sqrt{\frac{2E}{T}} \cos[2\pi f_c t + \pi], \quad 0 \leq t \leq T\end{aligned}$$

However, due to an imperfect phase modulator, the two signal waveforms are

$$\begin{aligned}s_1(t) &= \sqrt{\frac{2E}{T}} \cos[2\pi f_c t], \quad 0 \leq t \leq T \\ s_2(t) &= \sqrt{\frac{2E}{T}} \cos[2\pi f_c t + \pi - \theta_e], \quad 0 \leq t \leq T\end{aligned}$$

where θ_e is a small phase error. Assume that the two signals occur with equal probability, for the imperfect PSK modulation with coherent detection, please find

- (a) The error probability in the presence of additive white Gaussian noise of zero mean and spectra density of $N_0/2$.
 - (b) Compare with a conventional binary PSK signal, the signal-to-noise ratio (SNR) penalty as a function of phase error.
6. In a differential phase-shift keying (DPSK) modulation, information is encoded in the phase difference of the following two signal waveforms in consecutive time intervals

$$\begin{aligned}s_1(t) &= \sqrt{\frac{2E}{T}} \cos[2\pi f_c t], \quad 0 \leq t \leq T \\ s_2(t) &= \sqrt{\frac{2E}{T}} \cos[2\pi f_c t + \pi], \quad 0 \leq t \leq T\end{aligned}$$

However, due to an imperfect phase modulator, the two signal waveforms are

$$\begin{aligned}s_1(t) &= \sqrt{\frac{2E}{T}} \cos[2\pi f_c t], \quad 0 \leq t \leq T \\ s_2(t) &= \sqrt{\frac{2E}{T}} \cos[2\pi f_c t + \pi - \theta_e], \quad 0 \leq t \leq T\end{aligned}$$

where θ_e is a small phase error. Please find the error probability of the DPSK signal with phase error in the presence of additive white Gaussian noise of zero mean and spectra density of $N_0/2$.