

## Microwave Circuits Review Quiz #6 solution 2017.1.3

1. Figure 1.1 is a 10dB attenuator at  $T_o=290^\circ\text{K}$  and Figure 1.2 is a 10dB amplifier at  $T_e=290^\circ\text{K}$ . Give the parameters, expressions and results in the following table. ( $k=1.38 \times 10^{-23} \text{J}^\circ\text{K}$ ,  $1 \text{J/sec}=1 \text{W}=10^3 \text{mW}$ )

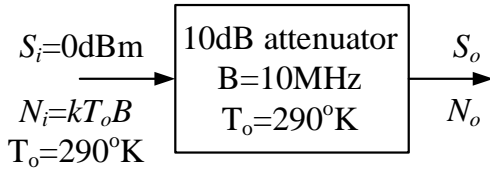


Fig. 1.1

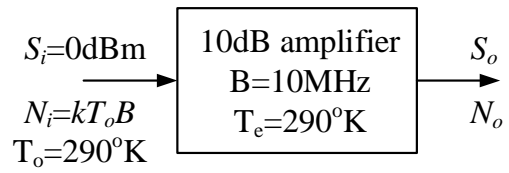


Fig. 1.2

| <i>10dB attenuator</i>     |   |   | <i>10dB amplifier</i>  |  |
|----------------------------|---|---|--|--|
| <i>Parameter</i>           | <i>Expression</i>   | <i>Result</i>   | <i>Expression</i>  | <i>Result</i>  |
| $N_i$ (W)                  | $kT_oB$   | $1.38 \times 10^{-23} \times 290 \times 10^7$<br>$= 4 \times 10^{-14} \text{W}$   | $kT_oB$  | $1.38 \times 10^{-23} \times 290 \times 10^7$<br>$= 4 \times 10^{-14} \text{W}$  |
| $N_i$ (dBm)                | $10 \log(N_i \times 10^3)$  | $10 \log(4 \times 10^{-11} \times 10^3)$<br>$= -104 \text{dBm}$   | $10 \log(N_i \times 10^3)$   | $10 \log(4 \times 10^{-11} \times 10^3)$<br>$= -104 \text{dBm}$  |
| $SNR_i$ (dB)               | $S_i(\text{dBm}) - N_i(\text{dBm})$                                       | $0 - (-104) = 104 \text{dB}$  | $S_i(\text{dBm}) - N_i(\text{dBm})$                                | $0 - (-104) = 104 \text{dB}$   |
| $G$<br>(power gain)        |   |   | $10^{\frac{S_o(\text{dB}) - S_i(\text{dB})}{10}}$<br>$= S_o / S_i$ | $10 \text{dB} = 10^{\frac{10(\text{dB})}{10}} = 10$  |
| $L$<br>(power loss)        | $10^{\frac{S_i(\text{dB}) - S_o(\text{dB})}{10}}$<br>$= S_i / S_o$        | $10 \text{dB} = 10^{\frac{10(\text{dB})}{10}}$<br>$= 10$  |  |  |
| $S_o$ (dBm)                | $S_i(\text{dBm}) - L(\text{dB})$  | $0 - 10 = -10 \text{dBm}$   | $S_i(\text{dBm}) + G(\text{dB})$                                   | $0 + 10 = 10 \text{dBm}$   |
| $T_e$ ( $^\circ\text{K}$ ) | $(L - 1)T_o$  | $(10 - 1) \times 290 = 2610^\circ \text{K}$   |  | $290^\circ \text{K}$   |
| $N_o$ (dBm)                | $N_i(\text{dBm})$<br>$(= 10 \log Gk(T_o + T_e)B)$<br>$= 10 \log GkT_oBF)$ | $-104 \text{dBm}$<br>$(= 10 \log[0.1 \times 1.38 \times 10^{-23} \times (290 + 2610) \times 10^7 \times 10^3])$<br>$= 10 \log[0.1 \times 1.38 \times 10^{-23} \times 290 \times 10^7 \times 10 \times 10^3]$<br>$= 10 \log[4 \times 10^{-11} (\text{mW})]$<br>$= -104 \text{dBm}$ | $10 \log Gk(T_o + T_e)B$   | $10 \log[10 \times 1.38 \times 10^{-23} \times (290 + 290) \times 10^7 \times 10^3]$<br>$= 10 \log[8 \times 10^{-10} (\text{mW})]$<br>$= -91 \text{dBm}$ |
| $SNR_o$ (dB)               | $S_o(\text{dBm}) - N_o(\text{dBm})$                                       | $-10 - (-104) = 94 \text{dB}$   | $S_o(\text{dBm}) - N_o(\text{dBm})$                                | $10 - (-91) = 101 \text{dB}$   |
| $F$ (dB)                   | $SNR_i$ (dB) - $SNR_o$ (dB)   | $104 - (94) = 10 \text{dB}$   | $SNR_i$ (dB) - $SNR_o$ (dB)  | $104 - (101) = 3 \text{dB}$  |
| $T_e$ ( $^\circ\text{K}$ ) |   |   | $(F - 1)T_o$   | $(2 - 1) \times 290 = 290^\circ \text{K}$  |