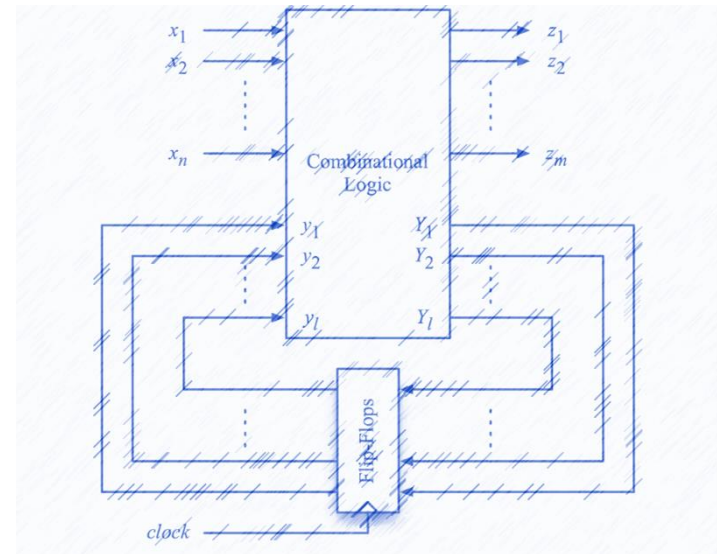


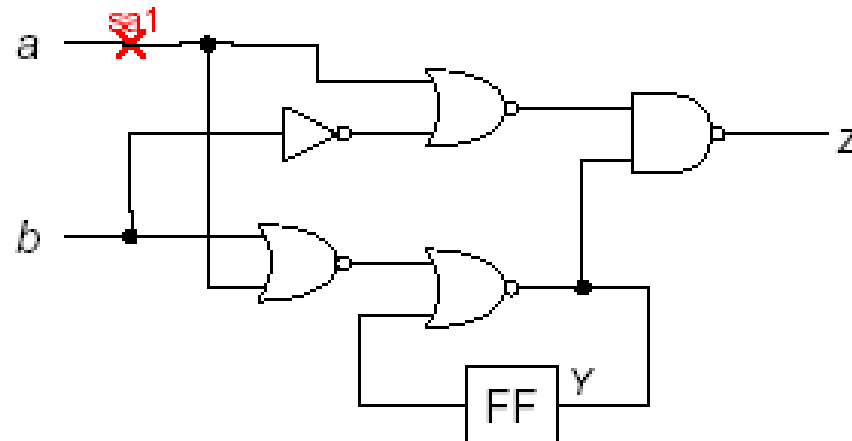
Sequential ATPG

- Introduction
- Time-frame expansion methods
 - ◆ The Extended D-algorithm [Kubo 68]
 - ◆ 9-valued D algorithm [Muth 76]
 - ◆ EBT [Marlett 78], BACK [Cheng 88] *
 - ◆ Summary
- Simulation-based methods*
- Issues of Sequential ATPG*
- Conclusions



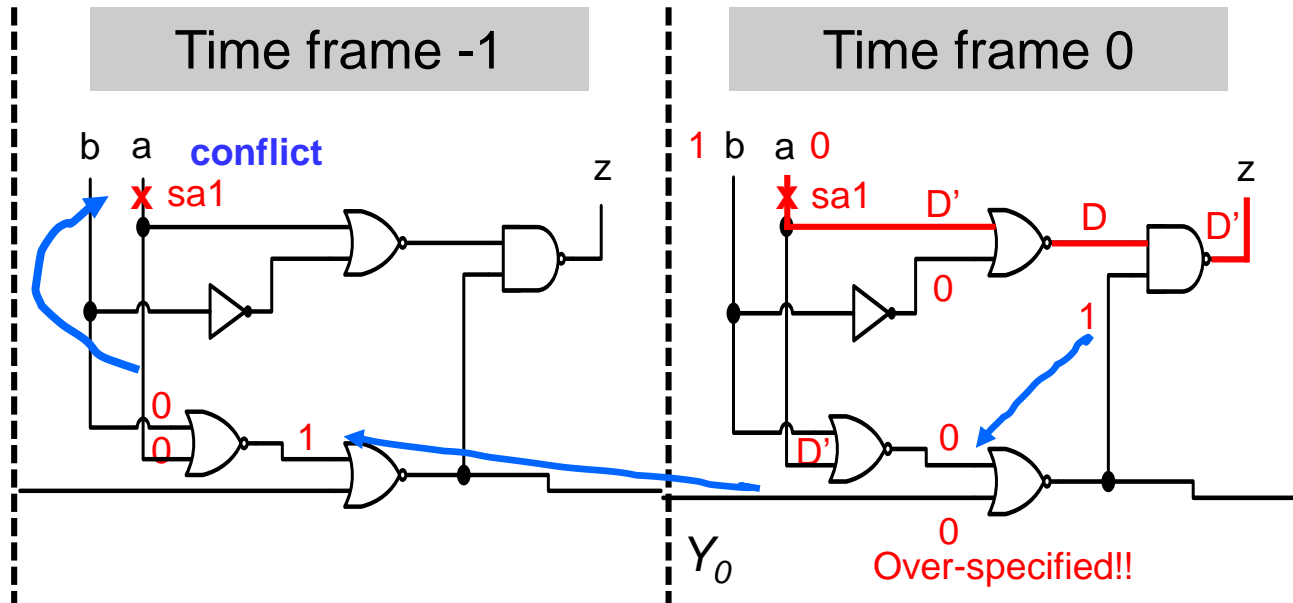
Quiz

Q: Given this test, can we detect the fault?
ANS:



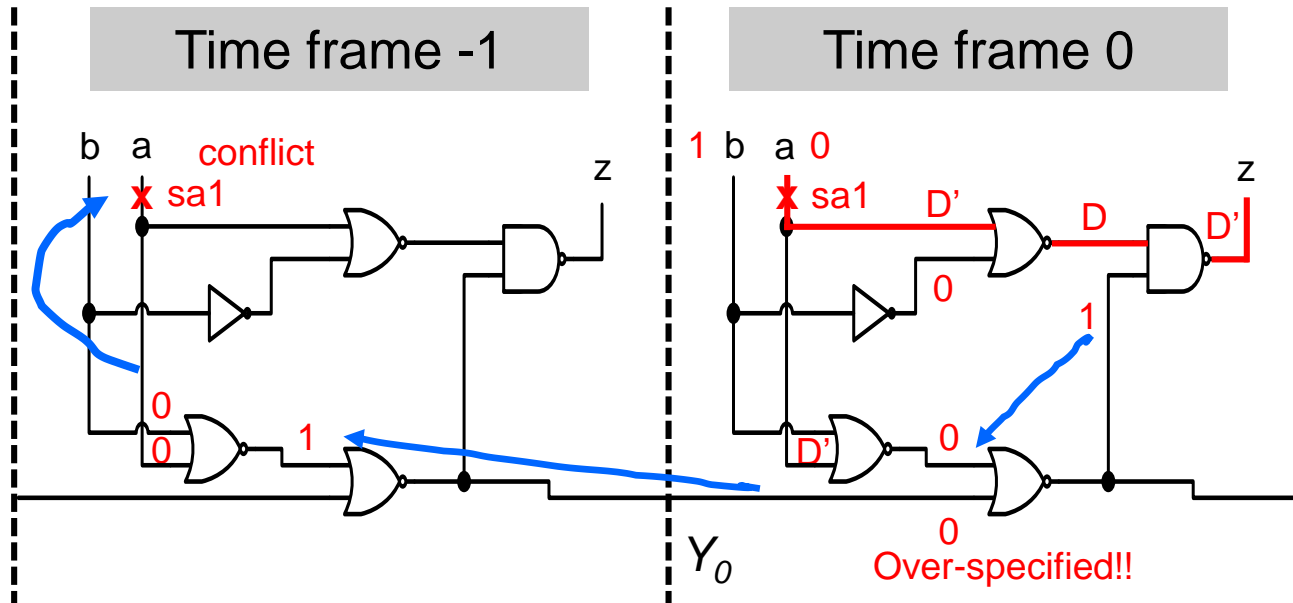
| | a | b |
|-------|-----|-----|
| v_1 | 0 | 0 |
| v_2 | 0 | 1 |

Extended D-algorithm Fails!



- Extended- D algorithm fails due to a conflict
 - ◆ Requires $a=0$ in time frame -1, but SA1
 - ◆ Actually, Y_0 is **over-specified** in 5-valued logic

Why Fails?



- Traditional 5-valued logic (0/0, 1/1, x/x, 0/1, 1/0) is **NOT** sufficient
 - ◆ cannot express **1/x, 0/x, x/0, x/1**

Q: How many total cases do we need?
ANS:

Nine-valued D-algorithm [Muth 76]

- Solution: use **9-valued logic**, instead of 5-valued logic

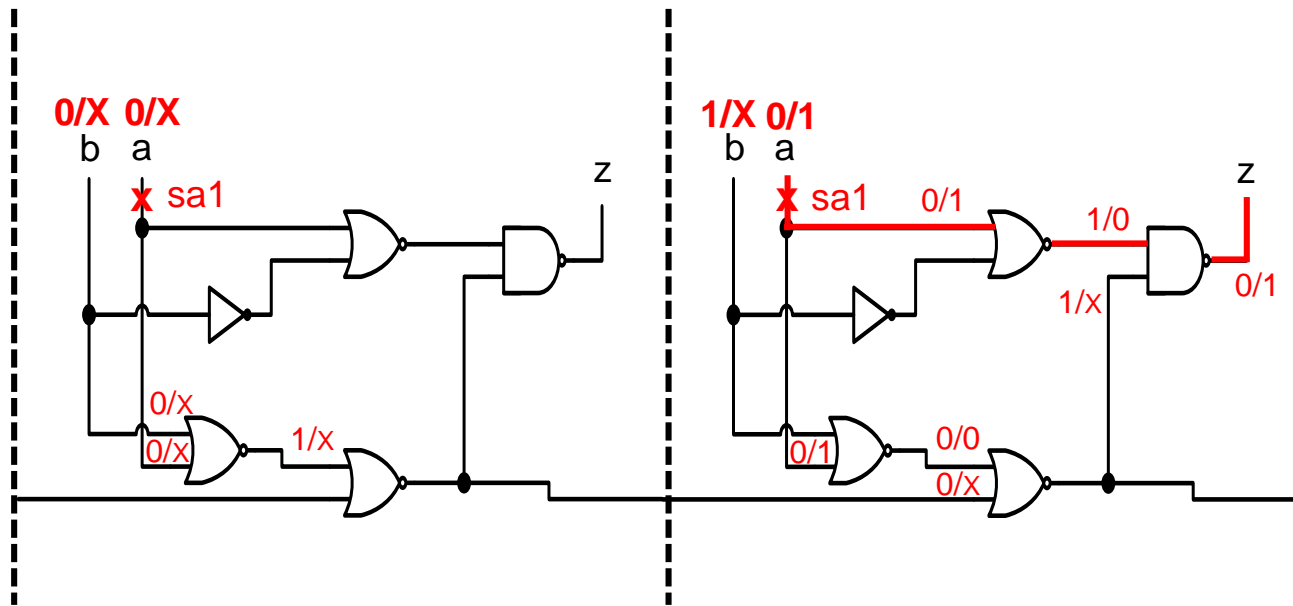
| Symbol | Meaning | Roth's 5-valued logic | | Muth's 9 valued logic | |
|--------|---------|-----------------------|--------|-----------------------|--------|
| | | Fault-free | faulty | Fault-free | faulty |
| D | (1/0) | 1 | 0 | 1 | 0 |
| D' | (0/1) | 0 | 1 | 0 | 1 |
| 0 | (0/0) | 0 | 0 | 0 | 0 |
| 1 | (1/1) | 1 | 1 | 1 | 1 |
| X | (x/x) | X | X | X | X |
| G0 | (0/x) | - | - | 0 | X |
| G1 | (1/x) | - | - | 1 | X |
| F0 | (x/0) | - | - | X | 0 |
| F1 | (x/1) | - | - | X | 1 |

Nine-valued Truth Table

- Example of AND gate

| AND | 0 | 0/x | D' | x/0 | x/x | x/1 | D | 1/x | 1 |
|-----|---|-----|-----|-----|-----|-----|-----|-----|-----|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0/x | 0 | 0/x | 0/x | 0 | 0/x | 0/x | 0 | 0/x | 0/x |
| D' | 0 | 0/x | D' | 0 | 0/x | D' | 0 | 0/x | D' |
| x/0 | 0 | 0 | 0 | x/0 | x/0 | x/0 | x/0 | x/0 | x/0 |
| x/x | 0 | 0/x | 0/x | x/0 | x/x | x/x | x/0 | x/x | x/x |
| x/1 | 0 | 0/x | D' | x/0 | x/x | x/1 | x/0 | x/x | x/1 |
| D | 0 | 0 | 0 | x/0 | x/0 | x/0 | D | D | D |
| 1/x | 0 | 0/x | 0/x | x/0 | x/x | x/x | D | 1/x | 1/x |
| 1 | 0 | 0/x | D' | x/0 | x/x | x/1 | D | 1/x | 1 |

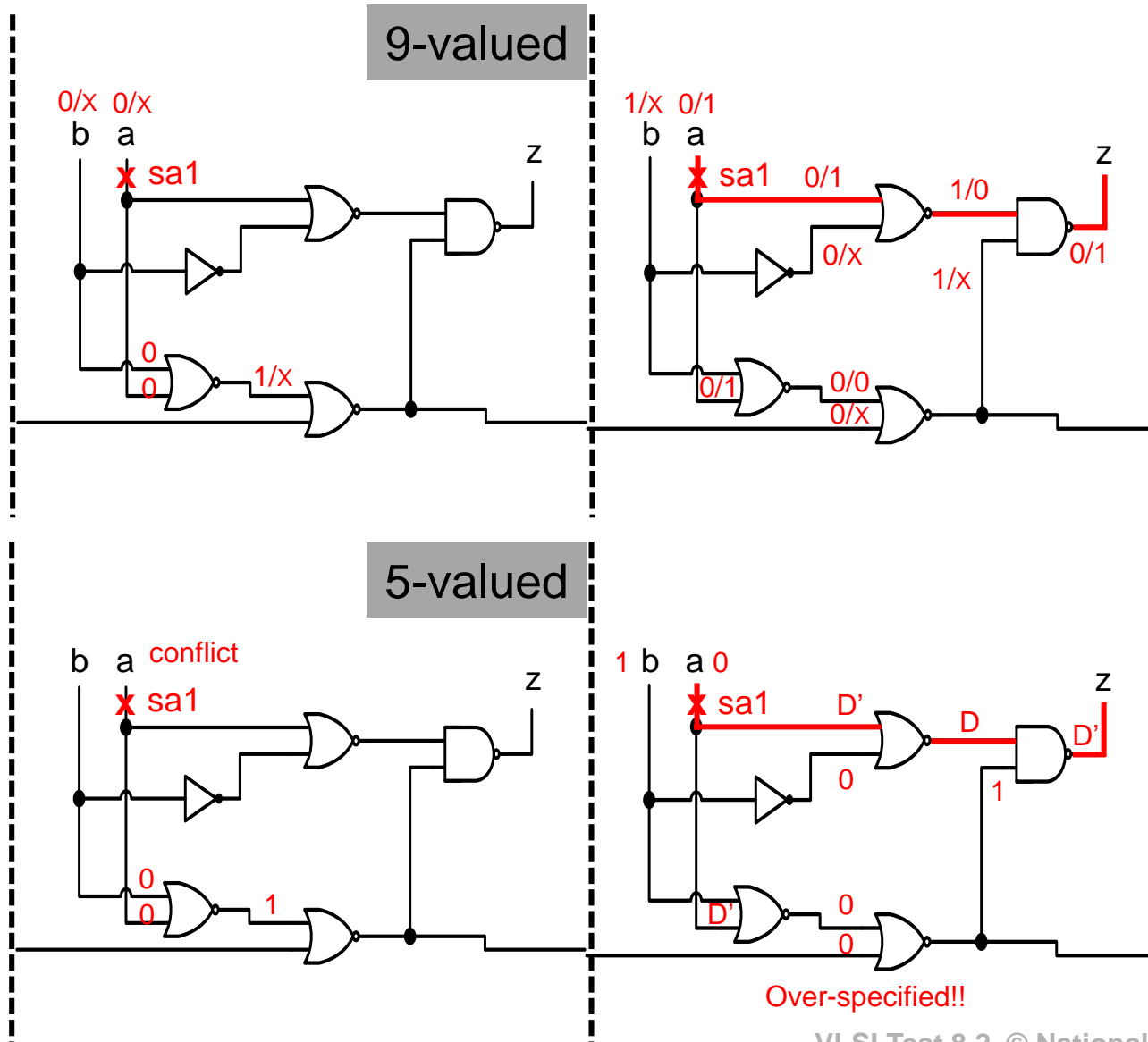
Nine-Valued Test Generation



Test pattern successfully generated

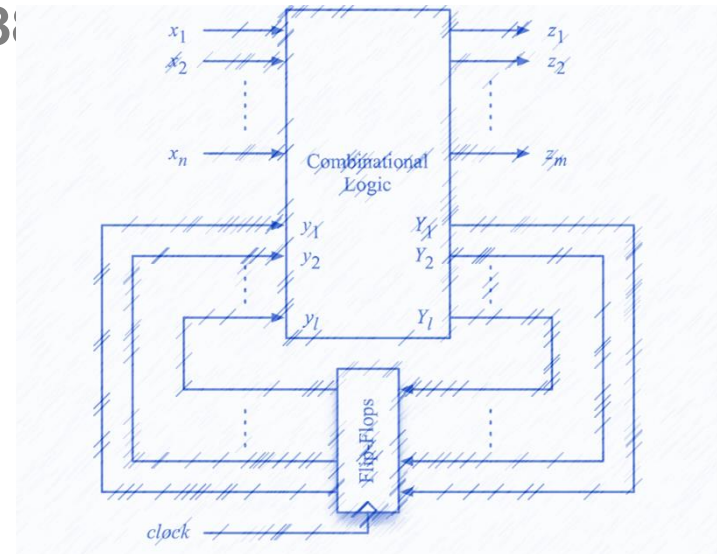
| | a | b |
|----------------|---|---|
| V ₁ | 0 | 0 |
| V ₂ | 0 | 1 |

Comparison: 9 v.s. 5 valued



Sequential ATPG

- Introduction
- Time-frame expansion methods
 - ◆ The Extended D-algorithm [Kubo 68]
 - ◆ 9-valued D algorithm [Muth 76]
 - express **all nine** possible logic states
 - avoid **over-specification**
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FFT

- Q1: Why **NOT** consider $1/x$, $0/x$, $x/0$, $x/1$ in combinational ATPG?
- Q2: Why **NOT** **backtrace** Y_{-1} one more time frame to the left?

